

# Contents

## PREFACE

## PART I LANGUAGE AND METHODS 1

---

### CHAPTER 1 SETS AND MAPPINGS 3

---

#### 1.1 Elements of Logic 3

- |                                 |   |
|---------------------------------|---|
| 1.1.1 Necessity and Sufficiency | 3 |
| 1.1.2 Theorems and Proofs       | 4 |

#### 1.2 Elements of Set Theory 5

- |                                   |    |
|-----------------------------------|----|
| 1.2.1 Notation and Basic Concepts | 5  |
| 1.2.2 Convex Sets                 | 7  |
| 1.2.3 Relations and Functions     | 11 |

#### 1.3 A Little Topology 13

- |                               |    |
|-------------------------------|----|
| 1.3.1 Continuity              | 22 |
| 1.3.2 Some Existence Theorems | 27 |

#### 1.4 Real Valued Functions 32

- |  |    |
|--|----|
| 1.4.1 Related Sets                     | 33 |
| 1.4.2 Concave Functions                | 36 |
| 1.4.3 Quasiconcave Functions           | 41 |
| 1.4.4 Convex and Quasiconvex Functions | 45 |

#### 1.5 Exercises 48

**CHAPTER 2 CALCULUS AND OPTIMIZATION****53**

|            |  |            |
|------------|--|------------|
| <b>2.1</b> | <b>Calculus</b>                            | <b>53</b>  |
| 2.1.1      | Functions of a Single Variable             | 53         |
| 2.1.2      | Functions of Several Variables             | 55         |
| 2.1.3      | Homogeneous Functions                      | 63         |
| <b>2.2</b> | <b>Optimization</b>                        | <b>66</b>  |
| 2.2.1      | Real Valued Functions of Several Variables | 68         |
| 2.2.2      | Second-Order Conditions                    | 71         |
| <b>2.3</b> | <b>Constrained Optimization</b>            | <b>77</b>  |
| 2.3.1      | Equality Constraints                       | 78         |
| 2.3.2      | Lagrange's Method                          | 79         |
| 2.3.3      | Geometrical Interpretation                 | 84         |
| 2.3.4      | Second-Order Conditions                    | 87         |
| 2.3.5      | Inequality Constraints                     | 91         |
| 2.3.6      | Kuhn-Tucker Conditions                     | 94         |
| <b>2.4</b> | <b>Value Functions</b>                     | <b>97</b>  |
| <b>2.5</b> | <b>Exercises</b>                           | <b>101</b> |

**PART II  
ECONOMIC AGENTS****107****CHAPTER 3 CONSUMER THEORY****109**

|            |   |            |
|------------|---|------------|
| <b>3.1</b> | <b>Primitive Notions</b>                | <b>109</b> |
| <b>3.2</b> | <b>Preferences and Utility</b>          | <b>111</b> |
| 3.2.1      | Preference Relations                    | 111        |
| 3.2.2      | The Utility Function                    | 119        |
| <b>3.3</b> | <b>The Consumer's Problem</b>           | <b>125</b> |
| <b>3.4</b> | <b>Indirect Utility and Expenditure</b> | <b>133</b> |
| 3.4.1      | The Indirect Utility Function           | 133        |
| 3.4.2      | The Expenditure Function                | 138        |
| 3.4.3      | Relations Between the Two               | 145        |
| <b>3.5</b> | <b>Properties of Consumer Demand</b>    | <b>151</b> |
| 3.5.1      | Relative Prices and Real Income         | 152        |

|       |                                 |     |
|-------|---------------------------------|-----|
| 3.5.2 | Income and Substitution Effects | 153 |
| 3.5.3 | Some Elasticity Relations       | 162 |

|            |                  |            |
|------------|------------------|------------|
| <b>3.6</b> | <b>Exercises</b> | <b>165</b> |
|------------|------------------|------------|

---

|                  |                                  |            |
|------------------|----------------------------------|------------|
| <b>CHAPTER 4</b> | <b>TOPICS IN CONSUMER THEORY</b> | <b>173</b> |
|------------------|----------------------------------|------------|

---

|            |                |            |
|------------|----------------|------------|
| <b>4.1</b> | <b>Duality</b> | <b>173</b> |
|------------|----------------|------------|

|       |   |     |
|-------|---|-----|
| 4.1.1 | Expenditure and Consumer Preferences      | 174 |
| 4.1.2 | Convexity and Monotonicity                | 178 |
| 4.1.3 | Indirect Utility and Consumer Preferences | 180 |

|            |                      |            |
|------------|----------------------|------------|
| <b>4.2</b> | <b>Integrability</b> | <b>184</b> |
|------------|----------------------|------------|

|            |                            |            |
|------------|----------------------------|------------|
| <b>4.3</b> | <b>Revealed Preference</b> | <b>189</b> |
|------------|----------------------------|------------|

|            |                    |            |
|------------|--------------------|------------|
| <b>4.4</b> | <b>Uncertainty</b> | <b>195</b> |
|------------|--------------------|------------|

|       |                                 |     |
|-------|---------------------------------|-----|
| 4.4.1 | Preferences                     | 195 |
| 4.4.2 | Von Neumann-Morgenstern Utility | 199 |
| 4.4.3 | Risk Aversion                   | 207 |

|            |                  |            |
|------------|------------------|------------|
| <b>4.5</b> | <b>Exercises</b> | <b>214</b> |
|------------|------------------|------------|

---

|                  |                           |            |
|------------------|---------------------------|------------|
| <b>CHAPTER 5</b> | <b>THEORY OF THE FIRM</b> | <b>218</b> |
|------------------|---------------------------|------------|

---

|            |                          |            |
|------------|--------------------------|------------|
| <b>5.1</b> | <b>Primitive Notions</b> | <b>218</b> |
|------------|--------------------------|------------|

|            |                   |            |
|------------|-------------------|------------|
| <b>5.2</b> | <b>Production</b> | <b>219</b> |
|------------|-------------------|------------|

|       |  |     |
|-------|--|-----|
| 5.2.1 | Returns to Scale and Varying Proportions | 224 |
|-------|--|-----|

|            |             |            |
|------------|-------------|------------|
| <b>5.3</b> | <b>Cost</b> | <b>227</b> |
|------------|-------------|------------|

|            |                              |            |
|------------|------------------------------|------------|
| <b>5.4</b> | <b>Duality in Production</b> | <b>235</b> |
|------------|------------------------------|------------|

|            |                             |            |
|------------|-----------------------------|------------|
| <b>5.5</b> | <b>The Competitive Firm</b> | <b>236</b> |
|------------|-----------------------------|------------|

|       |                     |     |
|-------|---------------------|-----|
| 5.5.1 | Profit Maximization | 236 |
| 5.5.2 | The Profit Function | 238 |

|            |                  |            |
|------------|------------------|------------|
| <b>5.6</b> | <b>Exercises</b> | <b>244</b> |
|------------|------------------|------------|

**PART III  
MARKETS AND WELFARE** **251****CHAPTER 6 PARTIAL EQUILIBRIUM** **253**

|            |   |            |
|------------|---|------------|
| <b>6.1</b> | <b>Perfect Competition</b>                | <b>253</b> |
| <b>6.2</b> | <b>Imperfect Competition</b>              | <b>257</b> |
| 6.2.1      | Cournot Oligopoly                         | 260        |
| 6.2.2      | Bertrand Oligopoly                        | 262        |
| 6.2.3      | Monopolistic Competition                  | 263        |
| <b>6.3</b> | <b>Equilibrium and Welfare</b>            | <b>265</b> |
| 6.3.1      | Price and Individual Welfare              | 266        |
| 6.3.2      | Efficiency of the Competitive Outcome     | 270        |
| 6.3.3      | Efficiency and Total Surplus Maximization | 272        |
| <b>6.4</b> | <b>Exercises</b>                          | <b>274</b> |

**CHAPTER 7 GENERAL EQUILIBRIUM** **280**

|            |  |            |
|------------|--|------------|
| <b>7.1</b> | <b>Equilibrium in Exchange</b>                   | <b>280</b> |
| <b>7.2</b> | <b>Equilibrium in Competitive Market Systems</b> | <b>286</b> |
| 7.2.1      | Existence of Equilibrium                         | 286        |
| <b>7.3</b> | <b>Equilibrium in Production</b>                 | <b>302</b> |
| 7.3.1      | Producers  | 302        |
| 7.3.2      | Consumers  | 305        |
| 7.3.3      | Equilibrium                                      | 306        |
| 7.3.4      | Welfare  | 313        |
| <b>7.4</b> | <b>Core and Equilibria</b>                       | <b>317</b> |
| 7.4.1      | Replica Economies                                | 318        |
| <b>7.5</b> | <b>Exercises</b>                                 | <b>328</b> |

**CHAPTER 8 SOCIAL CHOICE AND WELFARE** **334**

|            |                                  |            |
|------------|----------------------------------|------------|
| <b>8.1</b> | <b>The Nature of the Problem</b> | <b>334</b> |
|------------|----------------------------------|------------|

|   |   |            |
|---|---|------------|
| <b>8.2</b>                                | <b>Social Choice and Arrow's Theorem</b>                          | <b>335</b> |
| 8.2.1                                     | A Diagrammatic Proof  | 341        |
| <b>8.3</b>                                | <b>Measurability, Comparability, and Some Possibilities</b>       | <b>346</b> |
| 8.3.1                                     | The Rawlsian Form   | 348        |
| 8.3.2                                     | The Utilitarian Form  | 351        |
| 8.3.3                                     | Flexible Forms  | 352        |
| <b>8.4</b>                                | <b>Justice</b>  | <b>354</b> |
| <b>8.5</b>                                | <b>Exercises</b>  | <b>356</b> |
| <b>PART IV</b>                            |   |            |
| <b>STRATEGIC BEHAVIOR</b>                 |   | <b>361</b> |
| <hr/> <b>CHAPTER 9</b> <b>Game Theory</b> |   | <b>363</b> |
| <b>9.1</b>                                | <b>Strategic Decision Making</b>                                  | <b>363</b> |
| <b>9.2</b>                                | <b>Strategic Form Games</b>                                       | <b>365</b> |
| 9.2.1                                     | Dominant Strategies   | 366        |
| 9.2.2                                     | Nash Equilibrium  | 369        |
| 9.2.3                                     | Incomplete Information  | 376        |
| <b>9.3</b>                                | <b>Extensive Form Games</b>                                       | <b>381</b> |
| 9.3.1                                     | Game Trees: A Diagrammatic Representation                         | 384        |
| 9.3.2                                     | An Informal Analysis of Take-Away                                 | 385        |
| 9.3.3                                     | Extensive Form Game Strategies                                    | 387        |
| 9.3.4                                     | Strategies and Payoffs  | 388        |
| 9.3.5                                     | Games of Perfect Information<br>and Backward Induction Strategies | 389        |
| 9.3.6                                     | Games of Imperfect Information<br>and Subgame Perfect Equilibrium | 393        |
| 9.3.7                                     | Sequential Equilibrium  | 402        |
| <b>9.4</b>                                | <b>Exercises</b>  | <b>418</b> |

---

**CHAPTER 10 INFORMATION ECONOMICS** **424**

|                            |   |            |
|----------------------------|---|------------|
| <b>10.1</b>                | <b>Adverse Selection</b>                            | <b>425</b> |
| 10.1.1                     | Information and the Efficiency of Market Outcomes   | 425        |
| 10.1.2                     | Signaling   | 430        |
| 10.1.3                     | Screening   | 448        |
| <b>10.2</b>                | <b>Moral Hazard and the Principal Agent Problem</b> | <b>456</b> |
| 10.2.1                     | Symmetric Information                               | 457        |
| 10.2.2                     | Asymmetric Information                              | 459        |
| <b>10.3</b>                | <b>Information and Market Performance</b>           | <b>463</b> |
| <b>10.4</b>                | <b>Exercises</b>                                    | <b>463</b> |
| <b>LIST OF THEOREMS</b>    |   | <b>467</b> |
| <b>LIST OF DEFINITIONS</b> |   | <b>473</b> |
| <b>HINTS AND ANSWERS</b>   |   | <b>477</b> |
| <b>REFERENCES</b>          |   | <b>485</b> |
| <b>INDEX</b>               |   | <b>489</b> |