

Wolfgang Demtröder

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# Laser Spectroscopy

Basic Concepts  
and Instrumentation

Third Edition

With 710 Figures, 16 Tables

93 Problems and Hints for Solution



Springer

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