

# **Contents**

<i>Preface</i> .....	ix
<i>Acknowledgments</i> .....	xiii
<b>I. Logic and Set Theory</b>	
1.1 Introduction.....	1
1.2 Statements and Open Sentences.....	1
Exercises 1.2.....	7
1.3 Sets.....	10
Exercises 1.3.....	16
1.4 Ordered Pairs and Relations.....	19
Exercises 1.4.....	28
1.5 Functions and Kindred Matters.....	31
Exercises 1.5.....	40
1.6 Axiom Systems and Methods of Proof.....	47
<b>II. The Natural Numbers</b>	
2.1 Introduction.....	55
2.2 Arithmetic.....	56
Exercises 2.2.....	68
2.3 Ordering.....	70
Exercises 2.3.....	75
<b>III. The Integers and the Rational Numbers</b>	
3.1 Introduction.....	77
3.2 Preliminaries.....	78
Exercises 3.2.....	88
3.3 Additional Topics.....	90
Exercises 3.3.....	102
3.4 The Rational Numbers and Ordered Fields.....	106
Exercises 3.4.....	118

## viii Contents

### **IV. The Real and Complex Numbers**

4.1	Introduction.....	123
4.2	Construction of $\mathbf{R}$ .....	124
	Exercises 4.2.....	138

### **V. Metric Spaces**

5.1	Introduction.....	147
5.2	Definition and Basic Properties.....	148
	Exercises 5.2.....	154
5.3	Openness, Closedness, and Neighborhood Systems.....	157
	Exercises 5.3.....	165
5.4	Continuous Functions.....	168
	Exercises 5.4.....	171

### **VI. Limits**

6.1	Introduction.....	173
	Exercise 6.1 .....	176
6.2	Generalized Limits.....	176
	Exercises 6.2.....	189
6.3	Some Examples.....	194
	Exercises 6.3.....	203

<b>References.....</b>	<b>211</b>
<b>Answers to Selected Exercises.....</b>	<b>213</b>

<i>Subject Index.....</i>	<b>215</b>
---------------------------	------------