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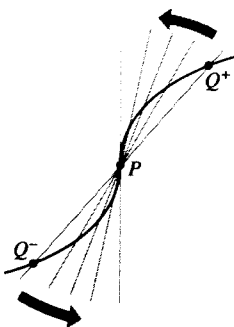
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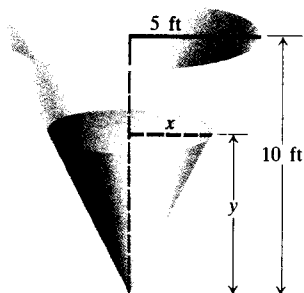
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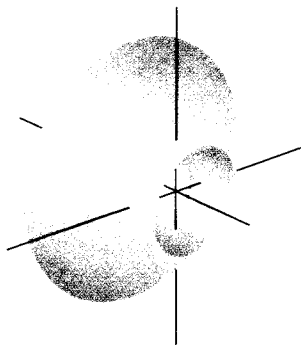


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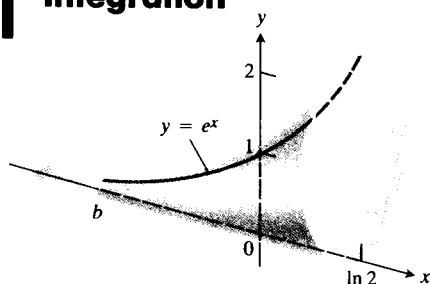


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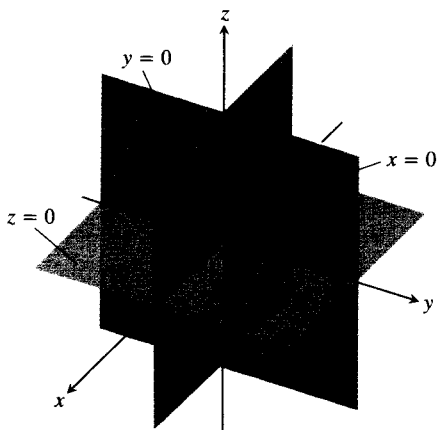
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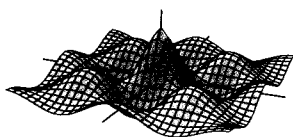


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$$z = (\cos x)(\cos y) e^{-\sqrt{x^2 + y^2}/4}$$

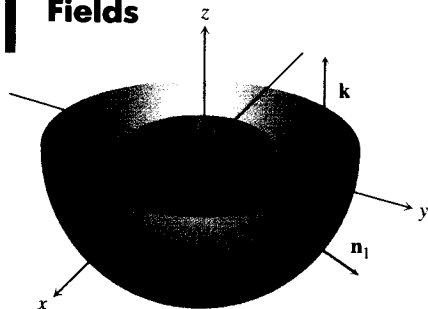
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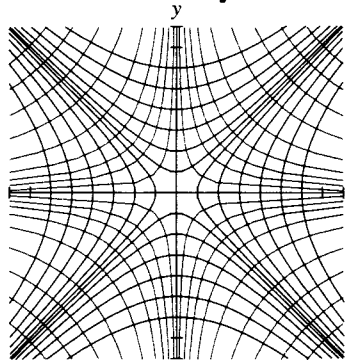
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