

THEORY AND APPLICATIONS OF HOLOMORPHIC FUNCTIONS
ON ALGEBRAIC VARIETIES OVER ARBITRARY GROUND FIELDS

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CONTENTS

Introduction

PART I. GENERAL THEORY OF HOLOMORPHIC FUNCTIONS

- § 1. Strongly holomorphic functions p. 12
§ 2. Strongly holomorphic functions on affine models p. 14
§ 3. The general concept of a holomorphic function p. 17
§ 4. Rational holomorphic functions. Some unsolved problems p. 21
§ 5. Digression on algebraic points p. 25
§ 6. Holomorphic functions, analytical irreducibility and a connectedness criterion p. 27
§ 7. Analytical irreducibility and normalization p. 34
§ 8. Some lemmas on \mathbb{C} -adic rings p. 38
§ 9. Holomorphic functions on affine models p. 40

PART II. INVARIANCE OF RINGS OF HOLOMORPHIC FUNCTIONS
UNDER RATIONAL TRANSFORMATIONS

- § 10. Holomorphic functions and semi-regular birational transformations p. 47
§ 11. Absolute birational invariance of rings of holomorphic functions p. 50
§ 12. Reduction of the proof of the fundamental theorem to a special case p. 52
§ 13. The birational transformation $V \dashrightarrow V_{\text{ot}}$ p. 55
§ 14. Proof of the fundamental theorem in the case of the transformation $V \dashrightarrow V_{\text{ot}}$ p. 59
§ 15. Last step of the proof: transition to the derived normal model $\overline{V_{\text{ot}}}$ p. 64
§ 16. Extension of the fundamental theorem to rational transformations p. 67
§ 17. Reduction of the proof to a special case p. 69
§ 18. The rational transformation $V \dashrightarrow V_{\text{ot}}$ p. 71
§ 19. The transformation $V_{\text{ot}} \dashrightarrow \overline{V_{\text{ot}}}$ p. 72

PART III. THE PRINCIPLE OF DEGENERATION

- § 20. A connectedness theorem for algebraic correspondences p. 77
§ 21. Algebraic systems of cycles p. 80
§ 22. Proof of the principle of degeneration p. 83