

# EXPLICIT FORMULAS FOR REGULARIZED PRODUCTS AND SERIES

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<b>Introduction</b>	<b>3</b>
<b>I Asymptotic estimates of regularized harmonic series</b>	<b>11</b>
1. Regularized products and harmonic series	14
2. Asymptotics in vertical strips	20
3. Asymptotics in sectors	22
4. Asymptotics in a sequence to the left	24
5. Asymptotics in a parallel strip	34
6. Regularized product and series type	36
7. Some examples	39
<b>II Cramér's Theorem as an Explicit Formula</b>	<b>43</b>
1. Euler sums and functional equations	45
2. The general Cramér formula	47
3. Proof of the Cramér theorem	51
4. An inductive theorem	57
<b>III Explicit Formulas under Fourier Assumptions</b>	<b>61</b>
1. Growth conditions on Fourier transforms	62
2. The explicit formulas	66
3. The terms with the $q$ 's	73
4. The term involving $\Phi$	78
5. The Weil functional and regularized product type	79
<b>IV From Functional Equations to Theta Inversions</b>	<b>85</b>
1. An application of the explicit formulas	87
2. Some examples of theta inversions	92

<b>V From Theta Inversions to Functional Equations</b>	<b>97</b>
1. The Weil functional of a Gaussian test function	99
2. Gauss transforms	101
3. Theta inversions yield zeta functions	109
4. A new zeta function for compact quotients of $M_3$	113
<b>VI A Generalization of Fujii's Theorem</b>	<b>119</b>
1. Statement of the generalized Fujii theorem	122
2. Proof of Fujii's theorem	125
3. Examples	128
<b>Bibliography</b>	<b>131</b>

**A SPECTRAL INTERPRETATION OF  
WEIL'S EXPLICIT FORMULA**

**Dorian Goldfeld**

1. Introduction	137
2. Notation	139
3. Construction of the indefinite space $\mathcal{L}^2(\Upsilon)$	140
4. Spectral theory of $\mathcal{L}^2(\Upsilon)$	141
5. Eisenstein series	142
6. Cusp forms	145
7. The zeta function associated to an automorphic form on $L^2(\Upsilon)$	147
8. The Rankin-Selberg convolution	148
9. Higher rank generalizations	148
10. References	152
<b>Index</b>	<b>153</b>