

# Table of contents

Preface .....	9
Acknowledgements .....	11
Notation .....	13
List of non-monotonic logics discussed in the book .....	19
<b>1 ELEMENTS OF MONOTONIC LOGICS .....</b>	<b>21</b>
<b>1.1 Basic notions .....</b>	<b>21</b>
<b>1.2 Classical propositional logic .....</b>	<b>26</b>
<b>1.2.1 Language of propositional logic .....</b>	<b>27</b>
<b>1.2.2. Semantics of propositional logic .....</b>	<b>28</b>
<b>1.2.3 Propositional theories .....</b>	<b>31</b>
<b>1.2.4 Propositional logic as a deduction system .....</b>	<b>33</b>
<b>1.3 Classical first-order logic .....</b>	<b>36</b>
<b>1.3.1 Language of first-order logic .....</b>	<b>36</b>
<b>1.3.2 Semantics of first-order logic .....</b>	<b>38</b>
<b>1.3.3 First-order theories .....</b>	<b>43</b>
<b>1.3.4 First-order logic as a deduction system .....</b>	<b>45</b>
<b>1.3.5 Many-sorted first-order logic .....</b>	<b>46</b>
<b>1.4 Resolution method .....</b>	<b>49</b>
<b>1.4.1 Clausal form .....</b>	<b>50</b>
<b>1.4.2 Resolution rule .....</b>	<b>53</b>
<b>1.4.3 Linear resolution .....</b>	<b>58</b>
<b>1.5 Classical second-order logic .....</b>	<b>60</b>
<b>1.5.1 Language of second-order logic .....</b>	<b>61</b>
<b>1.5.2 Semantics of second-order logic .....</b>	<b>62</b>
<b>1.5.3 Second-order theories .....</b>	<b>64</b>

## TABLE OF CONTENTS

<b>1.5.4 Deduction systems for second-order logic . . . . .</b>	64
<b>1.5.5 Predicate and function expressions . . . . .</b>	65
<b>1.6 Modal logic . . . . .</b>	69
<b>1.6.1 Modal propositional logic . . . . .</b>	69
<b>1.6.2 Modal first-order logic . . . . .</b>	73
<b>2 FOUNDATIONS OF NON-MONOTONIC REASONING . . . . .</b>	77
<b>2.1 Non-monotonic reasoning . . . . .</b>	77
<b>2.2 Non-monotonic inference and reasoning about action . . . . .</b>	82
<b>2.3 Typology of non-monotonic reasoning . . . . .</b>	84
<b>3 APPROACHES TO NON-MONOTONIC REASONING . . . . .</b>	88
<b>3.1 Computational approaches to non-monotonic reasoning . . . . .</b>	88
<b>3.1.1 MICRO-PLANNER . . . . .</b>	88
<b>3.1.2 Network- and frame-based systems . . . . .</b>	90
<b>3.1.3 Systems employing meta-level reasoning facilities . . . . .</b>	94
<b>3.1.4 Truth Maintenance systems . . . . .</b>	97
<b>3.2 Formal approaches to non-monotonic reasoning . . . . .</b>	102
<b>3.2.1 Sandewall's formalism . . . . .</b>	102
<b>3.2.2 Modal non-monotonic logics . . . . .</b>	103
<b>3.2.3 Default logic . . . . .</b>	103
<b>3.2.4 Circumscription . . . . .</b>	104
<b>3.2.5 Reasoning under the closed world assumption . . . . .</b>	105
<b>3.2.6 Poole's approach to non-monotonic reasoning . . . . .</b>	105
<b>3.2.7 Model-theoretic approach to non-monotonic reasoning . . . . .</b>	106
<b>3.3 Objections to non-monotonic formalisms . . . . .</b>	107
<b>4 MODAL NON-MONOTONIC LOGICS . . . . .</b>	111
<b>4.1 Modal non-monotonic logic of McDermott and Doyle . . . . .</b>	112
<b>4.2 Modal non-monotonic logics of McDermott . . . . .</b>	116
<b>4.3 Autoepistemic logic . . . . .</b>	122
<b>4.3.1 Preliminaries . . . . .</b>	122
<b>4.3.2 Semantic considerations . . . . .</b>	123
<b>4.3.3 Syntactic characterization of AE extensions . . . . .</b>	126
<b>4.3.4 Possible-world semantics for autoepistemic logic . . . . .</b>	133
<b>4.3.5 Reduction theorem . . . . .</b>	139
<b>4.3.6 Minimal, strongly grounded and superstrongly grounded AE extensions . . . . .</b>	141
<b>4.3.7 A comparison of autoepistemic logic to non-monotonic logics of McDermott and Doyle . . . . .</b>	145
<b>4.3.8 Conclusions . . . . .</b>	148
<b>4.4 Other bases for modal non-monotonic logic . . . . .</b>	149
<b>4.4.1 Intuitionistic basis for modal non-monotonic logic . . . . .</b>	149
<b>4.4.2 3-valued basis for modal non-monotonic logic . . . . .</b>	154
<b>5 DEFAULT LOGIC . . . . .</b>	159
<b>5.1 Preliminaries . . . . .</b>	160
<b>5.2 Open defaults and their instances . . . . .</b>	164
<b>5.3 Closed default theories . . . . .</b>	168
<b>5.4 Normal default theories . . . . .</b>	173

<b>5.5</b>	<b>Representational issues</b>	179
<b>5.6</b>	<b>Semi-normal default theories</b>	184
<b>5.7</b>	<b>Semantic characterization of extensions</b>	187
<b>5.8</b>	<b>Proof theory for closed normal default theories</b>	192
<b>5.9</b>	<b>A comparison between default logic and autoepistemic logic</b>	199
<b>5.10</b>	<b>Alternative formalization of default logic</b>	202
<b>5.11</b>	<b>Basic properties of the new formalization</b>	205
<b>5.12</b>	<b>Semantic characterization of m-extensions</b>	219
<b>5.13</b>	<b>Proof theory for alternative default logic</b>	224
<b>6</b>	<b>CIRCUMSCRIPTION</b>	226
<b>6.1</b>	<b>Introduction</b>	226
<b>6.2</b>	<b>Abnormality formalism</b>	228
<b>6.3</b>	<b>Predicate circumscription</b>	230
<b>6.3.1</b>	<b>Preliminaries</b>	230
<b>6.3.2</b>	<b>Semantics for predicate circumscription</b>	233
<b>6.3.3</b>	<b>Consistency of predicate circumscription</b>	238
<b>6.3.4</b>	<b>Expressive power of predicate circumscription</b>	239
<b>6.4</b>	<b>Formula circumscription</b>	241
<b>6.5</b>	<b>Second-order circumscription</b>	245
<b>6.5.1</b>	<b>Preliminaries</b>	245
<b>6.5.2</b>	<b>Satisfiability of second-order circumscription</b>	248
<b>6.5.3</b>	<b>Reducing second-order circumscription to first-order logic</b>	249
<b>6.5.4</b>	<b>Expressive power of second-order circumscription</b>	252
<b>6.5.5</b>	<b>Prioritized second-order circumscription</b>	254
<b>6.6</b>	<b>Non-recursive circumscription</b>	260
<b>6.7</b>	<b>Domain circumscription</b>	262
<b>6.8</b>	<b>Pointwise circumscription</b>	267
<b>6.8.1</b>	<b>The basic case</b>	267
<b>6.8.2</b>	<b>Minimizing several predicates</b>	269
<b>6.8.3</b>	<b>General pointwise circumscription</b>	271
<b>6.9</b>	<b>Conclusions</b>	277
<b>7</b>	<b>APPROACHES TO CLOSED WORLD ASSUMPTION</b>	281
<b>7.1</b>	<b>Introduction</b>	281
<b>7.2</b>	<b>Naive CWA</b>	282
<b>7.3</b>	<b>Generalized CWA</b>	288
<b>7.4</b>	<b>Careful CWA</b>	292
<b>7.5</b>	<b>Extended CWA</b>	297
<b>7.6</b>	<b>Theory completion</b>	300
<b>Bibliography</b>		309
<b>Index</b>		319