

Contents of Part II

Systems of Ordinary Differential Equations The Higher-Dimensional Theory $x' = f(t, x)$

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