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$$\int_{u=0} e^{-F(u)}(u-u_0)^{\sigma} G(u)du$$

and

$$\int_{\text{s.p.}} e^{-F(u)}(u-u_0)^{\sigma} G(u)du. \quad 255$$

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