

## C O N T E N T S

<u>1. General concepts.</u>	
1.1. Regular and singular perturbations . . . . .	1
1.2. Orders of magnitude. . . . .	9
1.3. Asymptotic approximations. Regular approximations in a subdomain. . . . .	13
1.4. Regular and local approximations . . . . .	21
1.5. Expansion operators for regular and local approximations .	30
1.6. Matching rules . . . . .	34
<u>2. Elementary heuristic reasoning in singular perturbations.</u>	
2.1. The elementary method of construction. . . . .	43
2.2. Application to linear ordinary differential equations with constant coefficients. . . . .	51
2.3. Application to linear ordinary differential equations with non-constant coefficients. . . . .	64
2.4. Remarks on the turning-point problem . . . . .	70
2.5. Linear elliptic problems without turning point . . . . .	75
2.5.1. The ordinary boundary layer . . . . .	79
2.5.2. The parabolic boundary layer. . . . .	83
2.5.3. The case of zeroth order unperturbed operator . . .	86
2.6. On non-linear problems . . . . .	90
<u>3. The structure of the approximations.</u>	
3.1. Failures of the elementary method. . . . .	97
3.2. Significant approximations . . . . .	107
3.3. Significant degenerations. . . . .	114
3.4. Relation between significant degenerations and significant approximations . . . . .	121
3.5. Application to problems of birth of boundary layers. . . .	127
3.6. The non-elementary terms and the construction of formal expansions by iteration. . . . .	135
<u>Bibliography.</u> . . . . .	143