

# Contents

Introduction . . . . .	1
Chapter XXV. Lagrangian Distributions and Fourier Integral Operators . . . . .	3
Summary . . . . .	3
25.1. Lagrangian Distributions . . . . .	4
25.2. The Calculus of Fourier Integral Operators . . . . .	17
25.3. Special Cases of the Calculus, and $L^2$ Continuity . . . . .	24
25.4. Distributions Associated with Positive Lagrangian Ideals . . . . .	35
25.5. Fourier Integral Operators with Complex Phase . . . . .	43
Notes . . . . .	52
Chapter XXVI. Pseudo-Differential Operators of Principal Type . . . . .	54
Summary . . . . .	54
26.1. Operators with Real Principal Symbols . . . . .	57
26.2. The Complex Involutive Case . . . . .	73
26.3. The Symplectic Case . . . . .	81
26.4. Solvability and Condition ( $\Psi$ ) . . . . .	91
26.5. Geometrical Aspects of Condition ( $P$ ) . . . . .	110
26.6. The Singularities in $N_{11}$ . . . . .	117
26.7. Degenerate Cauchy-Riemann Operators . . . . .	123
26.8. The Nirenberg-Treves Estimate . . . . .	134
26.9. The Singularities in $N_2^e$ and in $N_{12}^e$ . . . . .	137
26.10. The Singularities on One Dimensional Bicharacteristics . . . . .	149
26.11. A Semi-Global Existence Theorem . . . . .	161
Notes . . . . .	163
Chapter XXVII. Subelliptic Operators . . . . .	165
Summary . . . . .	165
27.1. Definitions and Main Results . . . . .	165
27.2. The Taylor Expansion of the Symbol . . . . .	171
27.3. Subelliptic Operators Satisfying ( $P$ ) . . . . .	178
27.4. Local Properties of the Symbol . . . . .	183

27.5. Local Subelliptic Estimates . . . . .	202
27.6. Global Subelliptic Estimates . . . . .	212
Notes . . . . .	219
Chapter XXVIII. Uniqueness for the Cauchy problem . . . . .	220
Summary . . . . .	220
28.1. Calderón's Uniqueness Theorem . . . . .	220
28.2. General Carleman Estimates . . . . .	234
28.3. Uniqueness Under Convexity Conditions . . . . .	239
28.4. Second Order Operators of Real Principal Type . . . . .	242
Notes . . . . .	248
Chapter XXIX. Spectral Asymptotics . . . . .	249
Summary . . . . .	249
29.1. The Spectral Measure and its Fourier Transform . . . . .	249
29.2. The Case of a Periodic Hamilton Flow . . . . .	263
29.3. The Weyl Formula for the Dirichlet Problem . . . . .	271
Notes . . . . .	274
Chapter XXX. Long Range Scattering Theory . . . . .	276
Summary . . . . .	276
30.1. Admissible Perturbations . . . . .	277
30.2. The Boundary Value of the Resolvent, and the Point Spectrum	281
30.3. The Hamilton Flow . . . . .	296
30.4. Modified Wave Operators . . . . .	308
30.5. Distorted Fourier Transforms and Asymptotic Completeness	314
Notes . . . . .	330
Bibliography . . . . .	332
Index . . . . .	350
Index of Notation . . . . .	352