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the cocktail party; expected values; game trees; The Petersburg Game; eternal happiness; the AHP consistency index; computing eigenvalues and eigenvectors; measuring areas and weighing bags with the AHP; conflict resolution and other uses of the AHP; establishing model validity; let's sing a song; and the last words.

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