## Contents

List	of tables	χv
List	of Figures	xix
Abl	previations for Education Systems	xxv
1.	Origins of the Second International Mathematics Study	
1.1	Introduction	1
1.2	Why a Second International Mathematics Study?	2
1.3	Conceptualization of the Study: Three Aspects of the Curriculum	5
1.4	Target Populations	10
1.5	Instrumentation	11
1.6	SIMS Management	12
2.	The International Grid and Item Pool	
2.1	A Framework for Describing the Curriculum	15
2.2	Behavioral Levels	19
2.3	The Content List	23
2.4	The International Grid: Population A	25
2.5	The International Grid: Population B	32
2.6	The International Item Pool	44
2.7	Summary	53
3.	National Characteristics of Educational Systems	
3.1	Population A	54
3.2	Target Populations and Age and Grade Cohorts	56
3.3	Placement of Population A Within School Systems	57
3.4	Class Size (Population A)	59
3.5	The Curricular Organization of Population A	60
3.6	Population B	63
3.7	Population B in the Context of Age and Grade Cohorts	66
3.8	The Curricular Organization of Population B	67
3.9	Class Size (Population B)	71

xii	Contents			
3.10 Curriculum Control				
	Curricular Diversity: A Typology	71 76		
	Summary	78		
4.	The Content of the Intended Curriculum			
4.1	Notation and Terminology	70		
4.2	Intended Content Coverage: Population A	79 83		
4.3	Curricular Clusters: Population A	93		
4.4	Intended Content Coverage: Population B	95 95		
4.5	Content Clusters: Population B	108		
4.6	Summary	110		
5.	The Content of the Implemented Mathematics Curriculum			
5.1	Introduction	111		
5.2	Measurement of Content Coverage: The Validity of OTL	113		
	5.2.1 Intended Coverage and Implemented Coverage	113		
	5.2.2 The Implemented Curriculum and Achievement	116		
5.3	Dimensions of the Implemented Curriculum	120		
5.4	Population A: Patterns of Content Coverage	123		
	5.4.1 Arithmetic: Between-system Patterns of Coverage	123		
	5.4.2 Arithmetic: Within-system Patterns of Coverage	124		
	5.4.3 Measurement: Between-system Patterns of Coverage	125		
	5.4.4 Measurement: Within-system Patterns of Coverage	125		
	5.4.5 Algebra: Between-system Patterns of Coverage	127		
	5.4.6 Algebra: Within-system Patterns of Coverage 5.4.7 Geometry: Between-system Patterns of Coverage	129		
		131		
	5.4.8 Geometry: Within-system Patterns of Coverage 5.4.9 Statistics: Between-system Patterns of Coverage	132		
		134		
5.5	5.4.10 Statistics: Within-system Patterns of Coverage	135		
5.6	Population A: Between-system Variation in Coverage Population A: Patterns of Within-system Variation	136		
5.7	Population B; Patterns of Content Coverage	139 147		
.,	5.7.1 Algebra: Between- and Within-system Patterns of	14/		
	Coverage	147		
	5.7.2 Elementary Functions and Calculus: Between-system	147		
	Patterns of Coverage	148		
	5.7.3 Elementary Functions and Calculus: Within-system	1.0		
	Patterns of Coverage	149		
	5.7.4 Number Systems: Between-system Patterns of Coverage	149		
	5.7.5 Number Systems: Within-system Patterns of Coverage	151		
	5.7.6 Geometry: Between-system Patterns of Coverage	153		
	5.7.7 Geometry: Within-system Patterns of Coverage	154		
	5.7.8 Sets and Relations, Probability and Statistics, and Finite			
<b>5</b> 0	Mathematics Parallel De Parall	156		
5.8	Population B: Between-system Variation in Coverage	160		
5.9 5.10	Population B: Patterns of Within-system Variation	160		
2.10	0 Summary 165			

		Content	s xiii	
6.	Outp	uts and Outcomes of Mathematics Education		
6.1	Introduction			
6.2	Yield			
6.3	Yield of Mathematics Education—Indicators			
6.4	The Context of Yield			
6.5	The Contexts of Population B Mathematics			
6.6	Gender-bias in Advanced Mathematics			
6.7	Yield	and Pace	187 191	
6.8	Sumn	nary	202	
7.	Sumi	nary and Implications		
7.1		Context of the Curriculum	203	
7.2		Content of the Curriculum: Population A	205	
	7.2.1		205	
	7.2.2	Curricular Diversity – Population A	207	
	7.2.3	Correspondence between Intended and Implemented		
		Curriculum: Population A	209	
7.3	The C	Content of the Curriculum: Population B	211	
	7.3.1	Commonality in the Population B Curriculum	211	
	7.3.2	Curricular Diversity – Population B	212	
	7.3.3	Correspondence between Intended and Implemented		
		Curriculum: Population B	214	
7.4	Yield	•	214	
	7.4.1	Illustrative Yield Data	216	
7.5	Mathe	ematics for All	218	
7.6	Postso	хipt	221	
Refe	rences		224	
Appendix I. Participating Systems				
Appendix II. Timeline for the Second International Mathematics Study				

233

Index