

# Table of Contents

<b>Chapter 1. Introduction . . . . .</b>	<b>1</b>
Dominique FRANÇOIS	
<b>Chapter 2. Constitutive Equations . . . . .</b>	<b>5</b>
Jean-Louis CHABOCHE	
2.1. Introduction . . . . .	5
2.2. Fundamental concepts . . . . .	6
2.2.1. Domain of elasticity . . . . .	6
2.2.2. Hardening . . . . .	8
2.2.3. Normality rules . . . . .	11
2.3. Unified theory of viscoplasticity . . . . .	13
2.3.1. General form of the constitutive law . . . . .	13
2.3.2. Choice of viscosity law . . . . .	14
2.3.3. Isotropic hardening laws . . . . .	16
2.3.4. Kinematic hardening laws . . . . .	18
2.3.5. Cyclic hardening and softening . . . . .	20
2.3.6. Static recovery . . . . .	20
2.3.7. Time-independent limit case . . . . .	21
2.3.8. Methods of determination . . . . .	22
2.3.8.1. Determination of hardening laws within independent time-scheme . . . . .	22
2.3.8.2. Determination of the viscosity law . . . . .	23
2.3.8.3. Determination of static recovery effects . . . . .	24
2.3.9. Other unified approaches . . . . .	24
2.4. Other types of modeling . . . . .	25
2.4.1. Plasticity-creep partition . . . . .	25
2.4.2. Methods by means of micro-macro transposition . . . . .	27
2.4.3. More advanced hardening laws . . . . .	30
2.4.4. Aging . . . . .	32

2.4.5. Damage . . . . .	33
2.5. Conclusion . . . . .	34
2.6. Bibliography . . . . .	35
<b>Chapter 3. Measurement of Elastic Constants . . . . .</b>	<b>41</b>
Pascal GADAUD	
3.1. Elastic constants . . . . .	42
3.1.1. The perfect crystal – elastic constants . . . . .	42
3.1.2. Isotropic solid – elastic moduli . . . . .	44
3.1.3. From isotropic solid to real material . . . . .	47
3.1.4. Dynamic modulus . . . . .	48
3.2. Quasi-static mechanical tests . . . . .	50
3.2.1. Uni-axial tensile and compression tests . . . . .	51
3.2.2. Torsion and bending tests . . . . .	52
3.2.3. Hydrostatic compression tests . . . . .	54
3.3. Ultrasonic methods . . . . .	55
3.3.1. Principle . . . . .	55
3.3.2. Measurement error sources . . . . .	56
3.3.3. Measurements at high temperatures . . . . .	57
3.3.4. Immersion-bath ultrasound interferometry . . . . .	59
3.4. Resonant methods . . . . .	60
3.4.1. Introduction to resonant methods . . . . .	60
3.4.2. Various experimental methods . . . . .	60
3.4.3. Bar and disk tests . . . . .	61
3.4.4. Bending tests on foil . . . . .	63
3.4.5. Torsion tests . . . . .	64
3.4.6. Other tests . . . . .	65
3.5. Modulus measurements of coatings . . . . .	65
3.5.1. Vibratory methods . . . . .	66
3.5.2. Instrumented indentation . . . . .	67
3.6. Bibliography . . . . .	69
<b>Chapter 4. Tensile and Compression Tests . . . . .</b>	<b>73</b>
Dominique FRANÇOIS	
4.1. Introduction . . . . .	73
4.2. Description of the tensile test . . . . .	73
4.2.1. Test piece . . . . .	73
4.2.2. Gripping . . . . .	74
4.2.3. Tensile testing machine . . . . .	74
4.2.3.1. Arrangements . . . . .	74
4.2.3.2. Stiffness . . . . .	76

4.3. Standard data . . . . .	77
4.4. Determination of constitutive equations . . . . .	79
4.4.1. True stress and strain . . . . .	79
4.4.2. Empirical expressions of the work hardening curve . . . . .	80
4.4.3. Necking . . . . .	83
4.4.3.1. Condition with no strain rate effect . . . . .	83
4.4.3.2. Strain rate sensitivity . . . . .	84
4.4.3.3. Yield drops . . . . .	85
4.5. Damage determination . . . . .	85
4.6. Compression test . . . . .	87
4.7. Conclusion . . . . .	87
4.8. Notations . . . . .	88
4.9. Bibliography . . . . .	88
<b>Chapter 5. Hardness Tests . . . . .</b>	<b>89</b>
Sylvie POMMIER	
5.1. Introduction . . . . .	89
5.2. Standard hardness tests . . . . .	90
5.2.1. Vickers hardness tests . . . . .	91
5.2.2. Micro-hardness . . . . .	92
5.2.3. Nano-hardness (Berkovich type indenter) . . . . .	92
5.2.4. Brinell and Rockwell ball tests . . . . .	93
5.3. Analytical approaches of hardness tests . . . . .	96
5.3.1. Identification of the modulus of elasticity (Hertz contact) . . . . .	96
5.3.2. Identification of the yield strength (Hill's analysis) . . . . .	100
5.4. Finite element analysis of hardness test . . . . .	103
5.4.1. Finite element method . . . . .	103
5.4.2. Effect of work-hardening amplitude . . . . .	105
5.4.3. Effect of the type of hardening . . . . .	106
5.4.4. Pile-up method . . . . .	107
5.4.5. Viscous material . . . . .	109
5.4.6. Porous materials . . . . .	110
5.4.7. Films and surface coatings . . . . .	111
5.4.8. Measurement of fracture toughness of brittle materials . . . . .	112
5.5. Conclusion . . . . .	112
5.6. Appendices . . . . .	113
5.6.1. Appendix 1: formulary (Hertz contact) . . . . .	113
5.6.2. Appendix 2: slip line method (Hill) . . . . .	118
5.6.3. Appendix 3: equivalences between tensile and hardness tests . . . . .	121
5.7. Bibliography . . . . .	121

<b>Chapter 6. Fatigue Tests . . . . .</b>	<b>125</b>
Henri-Paul LIEURADE, Suzanne DEGALLAIX, Gérard DEGALLAIX and Jean-Pierre GAUTHIER	
<b>6.1. Principles . . . . .</b>	<b>125</b>
6.1.1. Definition . . . . .	125
6.1.2. Objective of fatigue tests . . . . .	126
6.1.3. Classification of fatigue tests . . . . .	127
6.1.4. Classification of loading modes . . . . .	127
6.1.5. Test pieces . . . . .	128
6.1.5.1. Shape . . . . .	128
6.1.5.2. Dimensions . . . . .	128
6.1.5.3. Machining of test pieces . . . . .	128
6.1.6. Calibration of testing machines . . . . .	130
6.1.6.1. Definition of a dynamometric bar . . . . .	130
6.1.6.2. Determination of cyclic loads . . . . .	130
6.1.6.3. Dynamic calibration of testing machines by axial load . . . . .	130
6.2. High-cycle fatigue tests – endurance limit . . . . .	131
6.2.1. Classification of loadings . . . . .	131
6.2.2. Stress-number of cycles to failure curve (Wöhler curve) . . . . .	132
6.2.3. Nature and dispersion of fatigue test results . . . . .	133
6.2.4. Determination of endurance limit of metallic materials . . . . .	135
6.2.4.1. Estimation of fatigue resistance, $\sigma_D$ . . . . .	135
6.2.4.2. Statistical methods . . . . .	135
6.2.5. Expression of the S-N curve . . . . .	139
6.2.6. Estimation of the number of cycles $N_{50}$ by the Henry straight line method . . . . .	140
6.2.6.1. Field of application . . . . .	140
6.2.6.2. Principle of the method . . . . .	140
6.2.6.3. Implementation of the method . . . . .	141
6.2.7. Accounting for the main parameters of influence . . . . .	141
6.2.7.1. Mechanical parameters . . . . .	141
6.2.7.2. Geometric parameters . . . . .	144
6.2.7.3. Parameters of material processing . . . . .	146
6.2.7.4. Environmental parameters . . . . .	146
6.2.8. Examination of the fracture facies of the test pieces . . . . .	146
6.3. Low-cycle fatigue tests . . . . .	147
6.3.1. Introduction . . . . .	147
6.3.2. Physical mechanisms of low-cycle fatigue . . . . .	149
6.3.3. Methods for low-cycle fatigue tests . . . . .	152
6.3.4. Experimental apparatus . . . . .	153
6.3.4.1. Machines . . . . .	153
6.3.4.2. Test pieces . . . . .	154

6.3.4.3. Instrumentation . . . . .	154
6.3.5. Data processing . . . . .	156
6.3.5.1. Stress response: cyclic hardening/softening curves . . . . .	156
6.3.5.2. Stress-strain hysteresis loops . . . . .	163
6.3.5.3. Resistance to low-cycle fatigue curves . . . . .	165
6.3.6. Ratcheting effect . . . . .	167
6.4. Measurement of the crack propagation rate in fatigue. . . . .	168
6.4.1. Introduction . . . . .	168
6.4.1.1. Fatigue crack initiation and propagation . . . . .	168
6.4.1.2. Recalling the notion of plastic zone at the crack tip . . . . .	170
6.4.1.3. The Paris law . . . . .	171
6.4.1.4. Crack closure phenomenon . . . . .	172
6.4.2. Implementation of crack propagation rate measurements . . . . .	173
6.4.2.1. Principle of the test . . . . .	173
6.4.2.2. Test pieces . . . . .	174
6.4.2.3. Equipment . . . . .	176
6.4.2.4. Performing the test . . . . .	183
6.4.2.5. Processing and presentation of results. . . . .	185
6.4.2.6. Main information to deliver after the test. . . . .	188
6.4.3. Other types of tests . . . . .	188
6.4.3.1. Devices for testing outside ambient environment . . . . .	188
6.4.3.2. Variable loading tests . . . . .	188
6.4.3.3. Tests on non-metallic materials . . . . .	188
6.5. Bibliography . . . . .	189
<b>Chapter 7. Impact Tests . . . . .</b>	193
Jean-Michel FRUND	
7.1. Introduction. . . . .	193
7.2. Some history . . . . .	193
7.3. Description of the impact test . . . . .	194
7.3.1. Test piece . . . . .	194
7.3.2. Charpy impact pendulum . . . . .	196
7.3.3. Charpy instrumented impact pendulum. . . . .	196
7.3.3.1. Measurement of the load . . . . .	196
7.3.3.2. Measurement of the displacement . . . . .	197
7.3.3.3. Different time-displacement curves . . . . .	198
7.3.3.4. Determinations of the characteristic values of the load. . . . .	198
7.3.3.5. Determination of the global fracture energy . . . . .	198
7.3.3.6. Determination of the percentage of brittle appearance from the load-time curve . . . . .	200
7.4. Determination of transition curves . . . . .	200

7.5. Transition temperature and upper shelf . . . . .	201
7.6. Impact fracture energy-fracture toughness empirical correlations . . . . .	202
7.7. Bibliography . . . . .	205
<b>Chapter 8. Fracture Toughness Measurement . . . . .</b>	<b>207</b>
Dominique FRANÇOIS	
8.1. Introduction . . . . .	207
8.2. Fracture mechanics bases . . . . .	209
8.2.1. Rice Cherepanov J integral . . . . .	209
8.2.2. Stress intensity factor K . . . . .	210
8.2.3. Plastic zone at the crack tip . . . . .	211
8.2.3.1. Plastic zone correction . . . . .	211
8.2.3.2. Plane stress plastic zone . . . . .	212
8.2.3.3. Plane strain plastic zone . . . . .	213
8.3. Implementation of fracture toughness tests . . . . .	213
8.3.1. Test pieces . . . . .	213
8.3.2. Data processing . . . . .	215
8.3.3. Validity of measurements . . . . .	216
8.4. Measurement of fracture toughness $J_{lc}$ . . . . .	217
8.4.1. Basis of elastoplastic fracture mechanics . . . . .	217
8.4.2. $J_{lc}$ testing . . . . .	217
8.4.2.1. Interrupted loadings method . . . . .	218
8.4.2.2. Partial unloading method . . . . .	218
8.4.2.3. Potential drop method . . . . .	219
8.4.2.4. Other methods . . . . .	219
8.4.2.5. Crack tip blunting . . . . .	219
8.4.3. Data processing . . . . .	219
8.4.4. Conditions of validity . . . . .	220
8.5. CTOD measurement . . . . .	221
8.6. Conclusion . . . . .	221
8.7. Notations . . . . .	222
8.8. Bibliography . . . . .	222
<b>Chapter 9. Dynamic Tests . . . . .</b>	<b>225</b>
Jean-Luc LATAILLADE	
9.1. Introduction . . . . .	225
9.2. Test methods relying on propagation techniques and on the Hopkinson bar . . . . .	226
9.2.1. Compression device and uni-dimensional theory . . . . .	228
9.2.1.1. Radial inertia . . . . .	229
9.2.1.2. Calculation of applied load and of displacement . . . . .	230
9.2.1.3. Dynamic compression Hopkinson test . . . . .	231

9.2.2. Torsion with Hopkinson bars . . . . .	246
9.2.2.1. Overall considerations . . . . .	246
9.2.2.2. Case of very ductile materials . . . . .	249
9.2.3. Tension with Hopkinson bars . . . . .	251
9.2.3.1. Low resistance specimen adaptation . . . . .	251
9.2.3.2. Adaptation of a tensile test bench line for interrupted tests . . . . .	255
9.2.3.3. Brittle material case: alternatives . . . . .	256
9.2.4. Taylor test . . . . .	258
9.2.4.1. Overall considerations . . . . .	258
9.2.4.2. Principle . . . . .	259
9.3. Dynamic fracture mechanics tests . . . . .	259
9.3.1. Introduction . . . . .	259
9.3.2. Charpy test analysis according to the Kishimoto method . . . . .	260
9.3.3. Charpy test with Hopkinson bars . . . . .	262
9.4. Plate against plate test . . . . .	264
9.4.1. Principle . . . . .	264
9.4.1.1. Traveling diagram . . . . .	265
9.4.1.2. Rankine-Hugoniot conservation equation . . . . .	267
9.4.1.3. Lagrangian analysis . . . . .	270
9.4.1.4. Application to the characterization of an elastomer . . . . .	271
9.5. Collision tests . . . . .	277
9.5.1. Inertia wheel instrumented impacting device . . . . .	277
9.5.1.1. Overall considerations . . . . .	277
9.5.1.2. Discussion and application to an adhesive joint . . . . .	278
9.5.1.3. Application to an adhesive joint . . . . .	281
9.5.2. Drop weight tests . . . . .	284
9.5.2.1. Introduction: the critical mass-velocity couple . . . . .	284
9.6. Bibliography . . . . .	289
<b>Chapter 10. Notched Axi-symmetric Test Pieces . . . . .</b>	<b>293</b>
<b>Jacques BESSON</b>	
10.1. Introduction . . . . .	293
10.2. Geometry and notations . . . . .	294
10.3. Notch test piece testing . . . . .	296
10.3.1. Mechanical test . . . . .	296
10.3.2. Observation of damage . . . . .	297
10.4. Specimen elastic analysis . . . . .	297
10.5. Plastic analysis of specimens . . . . .	299
10.5.1. Bridgman analysis . . . . .	299
10.5.2. Finite element analysis . . . . .	303
10.5.3. Small deformations analysis . . . . .	304

10.5.4. Large deformations analysis. . . . .	305
10.5.4.1. Necked tensile specimen. . . . .	305
10.5.4.2. AE <sub>x</sub> specimens. . . . .	305
10.5.4.3. Plastic anisotropy . . . . .	306
10.6. Damage analysis . . . . .	308
10.6.1. Case study: brittle fracture. . . . .	310
10.6.2. Case study: uncoupled ductile fracture . . . . .	313
10.6.3. Case study: coupled ductile fracture . . . . .	316
10.7. Viscoplasticity and creep damage. . . . .	319
10.8. From notch to crack? . . . . .	320
10.9. Bibliography . . . . .	321
<b>List of Authors</b> . . . . .	325
<b>Index</b> . . . . .	327