

# Contents

<i>Preface</i>	v
1. Oscillator Model	1
1.1 Optical Susceptibility . . . . .	2
1.2 Absorption and Refraction . . . . .	6
1.3 Retarded Green's Function . . . . .	12
2. Atoms in a Classical Light Field	17
2.1 Atomic Optical Susceptibility . . . . .	17
2.2 Oscillator Strength . . . . .	21
2.3 Optical Stark Shift . . . . .	23
3. Periodic Lattice of Atoms	29
3.1 Reciprocal Lattice, Bloch Theorem . . . . .	29
3.2 Tight-Binding Approximation . . . . .	36
3.3 $k \cdot p$ Theory . . . . .	41
3.4 Degenerate Valence Bands . . . . .	45
4. Mesoscopic Semiconductor Structures	53
4.1 Envelope Function Approximation . . . . .	54
4.2 Conduction Band Electrons in Quantum Wells . . . . .	56
4.3 Degenerate Hole Bands in Quantum Wells . . . . .	60
5. Free Carrier Transitions	65
5.1 Optical Dipole Transitions . . . . .	65
5.2 Kinetics of Optical Interband Transitions . . . . .	69

5.2.1	Quasi- $D$ -Dimensional Semiconductors . . . . .	70
5.2.2	Quantum Confined Semiconductors with Subband Structure . . . . .	72
5.3	Coherent Regime: Optical Bloch Equations . . . . .	74
5.4	Quasi-Equilibrium Regime: Free Carrier Absorption . . . . .	78
6.	Ideal Quantum Gases	89
6.1	Ideal Fermi Gas . . . . .	90
6.1.1	Ideal Fermi Gas in Three Dimensions . . . . .	93
6.1.2	Ideal Fermi Gas in Two Dimensions . . . . .	97
6.2	Ideal Bose Gas . . . . .	97
6.2.1	Ideal Bose Gas in Three Dimensions . . . . .	99
6.2.2	Ideal Bose Gas in Two Dimensions . . . . .	101
6.3	Ideal Quantum Gases in $D$ Dimensions . . . . .	101
7.	Interacting Electron Gas	107
7.1	The Electron Gas Hamiltonian . . . . .	107
7.2	Three-Dimensional Electron Gas . . . . .	113
7.3	Two-Dimensional Electron Gas . . . . .	119
7.4	Multi-Subband Quantum Wells . . . . .	122
7.5	Quasi-One-Dimensional Electron Gas . . . . .	123
8.	Plasmons and Plasma Screening	129
8.1	Plasmons and Pair Excitations . . . . .	129
8.2	Plasma Screening . . . . .	137
8.3	Analysis of the Lindhard Formula . . . . .	140
8.3.1	Three Dimensions . . . . .	140
8.3.2	Two Dimensions . . . . .	143
8.3.3	One Dimension . . . . .	145
8.4	Plasmon Pole Approximation . . . . .	146
9.	Retarded Green's Function for Electrons	149
9.1	Definitions . . . . .	149
9.2	Interacting Electron Gas . . . . .	152
9.3	Screened Hartree–Fock Approximation . . . . .	156

10. Excitons	163
10.1 The Interband Polarization . . . . .	164
10.2 Wannier Equation . . . . .	169
10.3 Excitons . . . . .	173
10.3.1 Three- and Two-Dimensional Cases . . . . .	174
10.3.2 Quasi-One-Dimensional Case . . . . .	179
10.4 The Ionization Continuum . . . . .	181
10.4.1 Three- and Two-Dimensional Cases . . . . .	181
10.4.2 Quasi-One-Dimensional Case . . . . .	183
10.5 Optical Spectra . . . . .	184
10.5.1 Three- and Two-Dimensional Cases . . . . .	186
10.5.2 Quasi-One-Dimensional Case . . . . .	189
11. Polaritons	193
11.1 Dielectric Theory of Polaritons . . . . .	193
11.1.1 Polaritons without Spatial Dispersion and Damping . . . . .	195
11.1.2 Polaritons with Spatial Dispersion and Damping . .	197
11.2 Hamiltonian Theory of Polaritons . . . . .	199
11.3 Microcavity Polaritons . . . . .	206
12. Semiconductor Bloch Equations	211
12.1 Hamiltonian Equations . . . . .	211
12.2 Multi-Subband Microstructures . . . . .	219
12.3 Scattering Terms . . . . .	221
12.3.1 Intraband Relaxation . . . . .	226
12.3.2 Dephasing of the Interband Polarization . . . . .	230
12.3.3 Full Mean-Field Evolution of the Phonon-Assisted Density Matrices . . . . .	231
13. Excitonic Optical Stark Effect	235
13.1 Quasi-Stationary Results . . . . .	237
13.2 Dynamic Results . . . . .	246
13.3 Correlation Effects . . . . .	255
14. Wave-Mixing Spectroscopy	269
14.1 Thin Samples . . . . .	271
14.2 Semiconductor Photon Echo . . . . .	275

15. Optical Properties of a Quasi-Equilibrium Electron–Hole Plasma	283
15.1 Numerical Matrix Inversion . . . . .	287
15.2 High-Density Approximations . . . . .	293
15.3 Effective Pair-Equation Approximation . . . . .	296
15.3.1 Bound states . . . . .	299
15.3.2 Continuum states . . . . .	300
15.3.3 Optical spectra . . . . .	300
16. Optical Bistability	305
16.1 The Light Field Equation . . . . .	306
16.2 The Carrier Equation . . . . .	309
16.3 Bistability in Semiconductor Resonators . . . . .	311
16.4 Intrinsic Optical Bistability . . . . .	316
17. Semiconductor Laser	321
17.1 Material Equations . . . . .	322
17.2 Field Equations . . . . .	324
17.3 Quantum Mechanical Langevin Equations . . . . .	328
17.4 Stochastic Laser Theory . . . . .	335
17.5 Nonlinear Dynamics with Delayed Feedback . . . . .	340
18. Electroabsorption	349
18.1 Bulk Semiconductors . . . . .	349
18.2 Quantum Wells . . . . .	355
18.3 Exciton Electroabsorption . . . . .	360
18.3.1 Bulk Semiconductors . . . . .	360
18.3.2 Quantum Wells . . . . .	368
19. Magneto-Optics	371
19.1 Single Electron in a Magnetic Field . . . . .	372
19.2 Bloch Equations for a Magneto-Plasma . . . . .	375
19.3 Magneto-Luminescence of Quantum Wires . . . . .	378
20. Quantum Dots	383
20.1 Effective Mass Approximation . . . . .	383
20.2 Single Particle Properties . . . . .	386
20.3 Pair States . . . . .	388

20.4 Dipole Transitions . . . . .	392
20.5 Bloch Equations . . . . .	395
20.6 Optical Spectra . . . . .	396
21. Coulomb Quantum Kinetics	401
21.1 General Formulation . . . . .	402
21.2 Second Born Approximation . . . . .	408
21.3 Build-Up of Screening . . . . .	413
22. Quantum Optical Effects	421
22.1 Quantum Optics for Semiconductors . . . . .	421
22.2 Cluster Expansion . . . . .	424
22.2.1 Cluster Expansion for Fermions . . . . .	424
22.2.2 Quantum Optical Cluster Expansion . . . . .	428
22.3 Semiconductor Luminescence Equations . . . . .	429
22.4 Quasi-Stationary Luminescence . . . . .	432
Appendix A Field Quantization	437
A.1 Lagrange Functional . . . . .	437
A.2 Canonical Momentum and Hamilton Function . . . . .	442
A.3 Quantization of the Fields . . . . .	444
Appendix B Contour-Ordered Green's Functions	451
B.1 Interaction Representation . . . . .	452
B.2 Langreth Theorem . . . . .	455
B.3 Equilibrium Electron-Phonon Self-Energy . . . . .	458
<i>Index</i>	461