

# CONTENTS

<b>Series Editor's Foreword . . . . .</b>	xiii
<b>Preface . . . . .</b>	xv
<b>Notation . . . . .</b>	xix
<b>Chapter 1 Introduction</b>	
1.1 The Information-Handling Problem . . . . .	1
1.2 Basic Concepts of Pattern Recognition . . . . .	5
1.3 Fundamental Problems in Pattern Recognition System Design . . . . .	9
1.4 Design Concepts and Methodologies . . . . .	17
1.5 Examples of Automatic Pattern Recognition Systems . . . . .	21
1.6 A Simple Automatic Pattern Recognition Model . . . . .	36
<b>Chapter 2 Decision Functions</b>	
2.1 Introduction . . . . .	39
2.2 Linear Decision Functions . . . . .	40
2.3 Generalized Decision Functions . . . . .	48
2.4 Pattern Space and Weight Space . . . . .	53
2.5 Geometrical Properties . . . . .	55
2.5.1 Hyperplane Properties . . . . .	55
2.5.2 Dichotomies . . . . .	58
2.5.3 Dichotomization Capacity of Generalized Decision Functions . . . . .	60
2.6 Implementation of Decision Functions . . . . .	62
2.7 Functions of Several Variables . . . . .	64
2.7.1 Definitions . . . . .	65

2.7.2	Construction of Multivariate Functions . . . . .	67
2.7.3	Orthogonal and Orthonormal Systems of Functions	68
2.8	Concluding Remarks . . . . .	72
	References . . . . .	73
	Problems . . . . .	73

### **Chapter 3 Pattern Classification by Distance Functions**

3.1	Introduction . . . . .	75
3.2	Minimum-Distance Pattern Classification . . . . .	76
3.2.1	Single Prototypes . . . . .	77
3.2.2	Multiprototypes . . . . .	78
3.2.3	Extension of Minimum-Distance Classification Concepts . . . . .	81
3.2.4	A Design Example . . . . .	83
3.3	Cluster Seeking . . . . .	86
3.3.1	Measures of Similarity . . . . .	87
3.3.2	Clustering Criteria . . . . .	89
3.3.3	A Simple Cluster-Seeking Algorithm . . . . .	90
3.3.4	Maximin-Distance Algorithm . . . . .	92
3.3.5	$K$ -Means Algorithm . . . . .	94
3.3.6	Isodata Algorithm . . . . .	97
3.3.7	Evaluation of Clustering Results . . . . .	104
3.3.8	Graph-Theoretic Approach . . . . .	106
3.4	Unsupervised Pattern Recognition . . . . .	107
3.5	Concluding Remarks . . . . .	108
	References . . . . .	108
	Problems . . . . .	109

### **Chapter 4 Pattern Classification by Likelihood Functions**

4.1	Introduction . . . . .	110
4.2	Pattern Classification as a Statistical Decision Problem . . . . .	111
4.3	Bayes Classifier for Normal Patterns . . . . .	119
4.4	Error Probabilities . . . . .	124
4.5	A Family of Important Probability Density Functions . . . . .	130
4.6	Estimation of Probability Density Functions . . . . .	134
4.6.1	Form of the Probability Density Function . . . . .	134
4.6.2	Estimation of the Mean Vector and Covariance Matrix . . . . .	137
4.6.3	Bayesian Learning of the Mean Vector and Covariance Matrix . . . . .	139

4.6.4	Functional Approximation of Probability Density Functions . . . . .	145
4.7	Concluding Remarks . . . . .	154
	References . . . . .	155
	Problems . . . . .	156

## **Chapter 5 Trainable Pattern Classifiers—The Deterministic Approach**

5.1	Introduction . . . . .	158
5.2	The Perceptron Approach . . . . .	159
5.2.1	The Reward-Punishment Concept . . . . .	161
5.2.2	Proof of Convergence . . . . .	165
5.2.3	Variations of the Perceptron Approach . . . . .	168
5.3	Derivation of Pattern Classification Algorithms . . . . .	169
5.3.1	The Gradient Technique . . . . .	169
5.3.2	Perceptron Algorithm . . . . .	171
5.3.3	A Least-Mean-Square-Error Algorithm . . . . .	173
5.3.4	Convergence Proof of the LMSE Algorithm . . . . .	178
5.4	Multicategory Classification . . . . .	181
5.5	Learning and Generalization . . . . .	186
5.6	The Potential Function Approach . . . . .	187
5.6.1	Generation of Decision Functions . . . . .	188
5.6.2	Selection of Potential Functions . . . . .	193
5.6.3	Geometrical Interpretation and Weight Adjustment . . . . .	202
5.6.4	Convergence of Training Algorithms . . . . .	208
5.6.5	Multiclass Generalization . . . . .	212
5.7	Concluding Remarks . . . . .	213
	References . . . . .	214
	Problems . . . . .	215

## **Chapter 6 Trainable Pattern Classifiers—The Statistical Approach**

6.1	Introduction . . . . .	217
6.2	Stochastic Approximation Methods . . . . .	218
6.2.1	The Robbins-Monro Algorithm . . . . .	219
6.2.2	Speed of Convergence . . . . .	224
6.2.3	Multidimensional Extension . . . . .	225
6.3	Derivation of Pattern Classification Algorithms . . . . .	226
6.3.1	Estimation of Optimum Decision Functions by Stochastic Approximation Methods . . . . .	226
6.3.2	Increment-Correction Algorithm . . . . .	229

6.3.3 Least-Mean-Square-Error Algorithm . . . . .	233
6.4 The Method of Potential Functions . . . . .	235
6.5 Concluding Remarks . . . . .	239
References . . . . .	240
Problems . . . . .	241

## **Chapter 7 Pattern Preprocessing and Feature Selection**

7.1 Introduction . . . . .	243
7.2 Distance Measures . . . . .	247
7.3 Clustering Transformations and Feature Ordering . . . . .	250
7.4 Clustering in Feature Selection . . . . .	259
7.5 Feature Selection Through Entropy Minimization . . . . .	263
7.6 Feature Selection Through Orthogonal Expansions . . . . .	269
7.6.1 Review of the Fourier Series Expansion . . . . .	269
7.6.2 Karhunen-Loève Expansion . . . . .	271
7.7 Feature Selection Through Functional Approximation . . . . .	283
7.7.1 Functional Expansion . . . . .	283
7.7.2 Stochastic Approximation Formulation . . . . .	288
7.7.3 Kernel Approximation . . . . .	290
7.7.4 Use of Feature Functions in Classification . . . . .	291
7.8 Divergence Concept . . . . .	291
7.9 Feature Selection Through Divergence Maximization . . . . .	298
7.10 Binary Feature Selection . . . . .	307
7.10.1 A Sequential Algorithm . . . . .	308
7.10.2 A Parallel Algorithm . . . . .	310
7.11 Concluding Remarks . . . . .	313
References . . . . .	314
Problems . . . . .	314

## **Chapter 8 Syntactic Pattern Recognition**

8.1 Introduction . . . . .	316
8.2 Concepts From Formal Language Theory . . . . .	317
8.2.1 Definitions . . . . .	317
8.2.2 Types of Grammars . . . . .	320
8.3 Formulation of the Syntactic Pattern Recognition Problem	323
8.4 Syntactic Pattern Description . . . . .	324
8.5 Recognition Grammars . . . . .	328
8.5.1 Syntax-Directed Recognition . . . . .	328
8.5.2 Recognition of Graph-Like Patterns . . . . .	331
8.5.3 Recognition of Tree Structures . . . . .	339

8.6	Statistical Considerations . . . . .	340
8.6.1	Stochastic Grammars and Languages . . . . .	341
8.6.2	Learning the Production Probabilities . . . . .	343
8.7	Learning and Grammatical Inference. . . . .	350
8.7.1	Inference of String Grammars. . . . .	350
8.7.2	Inference of Two-Dimensional Grammars. . . . .	355
8.8	Automata as Pattern Recognizers . . . . .	357
8.9	Concluding Remarks . . . . .	360
	References . . . . .	361
	Problems . . . . .	361
	<b>Bibliography</b> . . . . .	363
	<b>Index</b> . . . . .	372