Contents

Introduction 1 References and Suggested Readings 8

Part I / Real Dynamic Macroeconomic Models

1. Dynamic Programming 11

A General Intertemporal Problem 12 A Recursive Problem 13 Bellman's Equations 16 Nonstochastic Examples 22 The Optimal Linear Regulator Problem 27 Stochastic Control Problems 29 Examples of Stochastic Control Problems 31 The Stochastic Linear Optimal Regulator Problem 36 Dynamic Programming and Lucas's Critique 40 Dynamic Games and the Time Inconsistency Phenomenon 41 Conclusions 47 Exercises 47 References and Suggested Readings 54

2. Search 57

Nonnegative Random Variables 58 Stigler's Model of Search 59 Sequential Search for the Lowest Price 60 Mean-Preserving Spreads 63 Increases in Risk and the Reservation Price 65

Sargent, Thomas J. Dynamic macroeconomic theory 1987 Intertemporal Job Search 65 Waiting Times 70 Firing 70 Jovanovic's Matching Model 71 Conclusions 83 Exercises 85 References and Suggested Readings 91

3. Asset Prices and Consumption 92

Hall's Random Walk Theory of Consumption 93 The Random Walk Theory of Stock Prices 94 Lucas's Model of Asset Prices 95 Mehra and Prescott's Finite-State Version of Lucas's Model 100 Asset Pricing More Generally 101 The Modigliani-Miller Theorem 115 Government Debt and the Ricardian Proposition 116 Remarks on Testing and Estimation 119 Conclusions 120 Exercises 121 References and Suggested Readings 128

Part II / Monetary Economics and Government Finance

4. Currency in the Utility Function 133

The Price of Inconvertible Government Currency in Lucas's Tree Model 133 Issues and Models in Monetary Economics 137 Government Debt in the Utility Function 140 Government Currency in the Utility Function 142 Seignorage and the Optimum Quantity of Currency 145 A Neutrality Proposition 148 Conclusions 152 References and Suggested Readings 153

5. Cash-in-Advance Models 155

A One-Country Model 156 Fisher Equations 165 Inflation-Indexed Government Debt 166 Interactions of Monetary and Fiscal Policies 168 Interest on Reserves 177 A Two-Country Model 182 Exchange Rate Indeterminacy 188 Conclusions 192 Exercises 192 References and Suggested Readings 198

6. Credit and Currency with Long-Lived Agents 199

The Physical Setup 200 Optimal Allocations 201 Competitive Equilibrium 202 A Digression on the Balances of Trade and Payments 207 The Ricardian Doctrine about Taxes and Government Debt 207 The Model with Valued Currency and No Private Debt 212 An Interventionist Optimal Monetary Equilibrium 220 Townsend's "Turnpike" Interpretation 224 Conclusions 226 Exercises 226 References and Suggested Readings 230

7. Credit and Currency with Overlapping Generations 231

The Overlapping-Generations Model 232 The Ricardian Doctrine about Taxes and Government Debt Again 244 A Ricardian Proposition 250 Currency, Bonds, and Open-Market Operations 253 Computing Equilibria 257 Interpretations as Currency Equilibria 264 Optimality 266 Four Examples on Inflation and Its Causes 269 Seignorage and the Laffer Curve 275 Dynamics of Seignorage 281 Forced Saving 283 International Exchange Rates 285 Conclusions 289 Exercises 290 References and Suggested Readings 301

8. Government Finance in Stochastic Overlapping-Generations Models 304

The Economy 305 Some Examples 309 A General Irrelevance Theorem 319 Wallace's Modigliani-Miller Theorem for Open-Market Operations 323 Chamley and Polemarchakis's Neutrality Theorem 324 Interpretation as a Constant Fiscal Policy 327 Indexed Government Bonds 328 A Ricardian Proposition 331 Further Irrelevance Theorems 333 Conclusions 333 Exercises 334 References and Suggested Readings 337

Appendix. Functional Analysis for Macroeconomics 339

Metric Spaces and Operators 340 First-Order Linear Difference Equations 345 A Formula of Hansen and Sargent 350 A Quadratic Optimization Problem in R^{∞} 352 A Discounted Quadratic Optimization Problem 354 Predicting a Geometric Distributed Lead of a Stochastic Process 357 Discounted Dynamic Programming 360 A Search Problem 361 Exercises 362 References and Suggested Readings 363

Index 365