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¹ Section 4.3 can be omitted without affecting the continuity of the remainder of the text.

² Section 6.5.3 can be omitted without affecting the continuity of the remainder of the text.

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