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# Theory of Modeling and Simulation

## Integrating Discrete Event and Continuous Complex Dynamic Systems

*Second Edition*

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**ACADEMIC PRESS**

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A Harcourt Science and Technology Company

San Diego San Francisco New York Boston  
London Sydney Tokyo

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