## Contents

Preface	pag	ge ix
Chapter 1	Algorithms on Words	1
1.0	Introduction	1
1.1	Words	3
1.2	Elementary algorithms	7
1.3	Tries and automata	15
1.4	Pattern matching	36
1.5	Transducers	40
1.6	Parsing	52
1.7	Word enumeration	69
1.8	Probability distributions on words	74
1.9	Statistics on words	91
	Problems	96
	Notes	101
Chapter 2	Structures for Indexes	106
2.0	Introduction	106
2.1	Suffix trie	107
2.2	Suffix tree	113
2.3	Contexts of factors	121
2.4	Suffix automaton	127
2.5	Compact suffix automaton	138
2.6	Indexes	141
2.7	Finding regularities	150
2.8	Pattern matching machine	155
	Problems	160
	Notes	161

vi Contents

Symbolic Natural Language Processing	164
Introduction	164
	165
From words to sentences	199
Notes	208
Statistical Natural Language Processing	210
Introduction	210
Preliminaries	211
Algorithms	213
Application to speech recognition	226
Notes	239
Inference of Network Expressions	241
Introduction	241
	242
•	248
	256
	260
	264
Notes	265
Statistics on Words with Applications to Biological	
Sequences	268
Introduction	268
	270
<u> </u>	277
	281
	289
Renewal count distribution	311
Occurrences and counts of multiple patterns	315
	328
	338
Notes	346
Analytic Approach to Pattern Matching	353
Introduction	353
Probabilistic models	356
	Statistical Natural Language Processing Introduction Preliminaries Algorithms Application to speech recognition Notes  Inference of Network Expressions Introduction Inferring simple network expressions: models and related problems Algorithms Inferring network expressions with spacers Related issues Open problems Notes  Statistics on Words with Applications to Biological Sequences Introduction Probabilistic models for biological sequences Overlapping and nonoverlapping occurrences Word locations along a sequence Word count distribution Renewal count distribution Occurrences and counts of multiple patterns Some applications to DNA sequences Some probabilistic and statistical tools Notes  Analytic Approach to Pattern Matching Introduction

Contents vii

7.0	T	359
7.2	Exact string matching	
7.3	Generalized string matching	375
7.4	Subsequence pattern matching	393
7.5	Generalized subsequence problem	407
7.6	Self-repetitive pattern matching	413
	Problems	425
	Notes	427
Chapter 8	Periodic Structures in Words	430
8.0	Introduction	430
8.1	Definitions and preliminary results	431
8.2	Counting maximal repetitions	433
8.3	Basic algorithmic tools	439
8.4	Finding all maximal repetitions in a word	443
8.5	Finding quasi-squares in two words	448
8.6	Finding repeats with a fixed gap	450
8.7	Computing local periods of a word	454
8.8	Finding approximate repetitions	461
0.0	Notes	474
	Notes	4/4
Chapter 9	Counting, Coding, and Sampling with Words	478
Chapter 9 9.0	Counting, Coding, and Sampling with Words	478 478
-		
9.0	Introduction	478
9.0 9.1	Introduction	478 480
9.0 9.1 9.2	Introduction	478 480 492 504
9.0 9.1 9.2	Introduction	478 480 492 504 516
9.0 9.1 9.2	Introduction	478 480 492 504
9.0 9.1 9.2	Introduction	478 480 492 504 516
9.0 9.1 9.2 9.3	Introduction	478 480 492 504 516 518
9.0 9.1 9.2 9.3 Chapter 10	Introduction	478 480 492 504 516 518
9.0 9.1 9.2 9.3 Chapter 10	Introduction	478 480 492 504 516 518
9.0 9.1 9.2 9.3 Chapter 10	Introduction	478 480 492 504 516 518 520
9.0 9.1 9.2 9.3 <b>Chapter 10</b> 10.0 10.1	Introduction	478 480 492 504 516 518 520 520
9.0 9.1 9.2 9.3 <b>Chapter 10</b> 10.0 10.1	Introduction	478 480 492 504 516 518 520 520 521
9.0 9.1 9.2 9.3 <b>Chapter 10</b> 10.0 10.1 10.2 10.3	Introduction	478 480 492 504 516 518 520 520
9.0 9.1 9.2 9.3 <b>Chapter 10</b> 10.0 10.1	Introduction	478 480 492 504 516 518 520 520 521 526
9.0 9.1 9.2 9.3 <b>Chapter 10</b> 10.0 10.1 10.2 10.3 10.4	Introduction .  Counting: walks in sectors of the plane .  Sampling: polygons, animals, and polyominoes .  Coding: trees and maps .  Problems .  Notes .  Words in Number Theory .  Introduction .  Morphic and automatic sequences: definitions and generalities .  d-Kernels and properties of automatic sequences .  Christol's algebraic characterization of automatic sequences .  An application to transcendence in positive characteristic .	478 480 492 504 516 518 520 520 521
9.0 9.1 9.2 9.3 <b>Chapter 10</b> 10.0 10.1 10.2 10.3	Introduction	478 480 492 504 516 518 520 520 521 526

V111	Co	ntents

10.7	The Tribonacci word	546
10.8	The Rauzy fractal	552
10.9	An application to simultaneous approximation	564
	Problems	567
	Notes	574
References		579
General In	dex	603