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"Begin at the beginning," the King said very gravely,
"and go on till you come to the end; then stop."
'Alice in Wonderland', Lewis Carroll

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