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Pharmaceutical Statistics

Practical and Clinical Applications

Third Edition

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CONTENTS

Preface		

i

1.	Basi	c Definitions and Concepts	1
	1.1	Variables and Variation	1
	1.2	Frequency Distributions and Cumulative Frequency	
		Distributions	5
	1.3	Sample and Population	12
	1.4	Measures Describing the Center of Data Distributions	14
	1.5	Measurement of the Spread of Data	20
	1.6	Coding	28
	1.7	Precision, Accuracy, and Bias	30
	1.8	The Question of Significant Figures	33
		Key Terms	35
		Exercises	35
		References	37
2.	Data	a Graphics	39
	2.1	Introduction	40
	2.2	The Histogram	41
	2.3	Construction and Labeling of Graphs	41
	2.4	Scatter Plots (Correlation Diagrams)	51
			vii

v

Со	nte	nts
----	-----	-----

	2.5	Semilogarithmic Plots	51
	2.6	Other Descriptive Figures	54
		Key lerms	28
		Exercises Deformers	
		References	01
3.	Intr Prol	oduction to Probability: The Binomial and Normal pability Distributions	62
	2 1	Texter duration	62
	3.1	Introduction Some Basic Probability	62 63
	3.2	Probability Distributions—The Binomial Distribution	68
	34	Continuous Data Distributions	78
	3.5	Other Common Probability Distributions	94
		Key Terms	98
		Exercises	98
		References	101
4.	Cho	osing Samples	102
	4.1	Introduction	102
	4.2	Random Sampling	104
	4.3	Other Sampling Procedures: Stratified, Systematic, and	
		Cluster Sampling	110
	4.4	Sampling in Quality Control	113
		Key Terms	116
		Exercises	110
		References	119
5.	Stat	istical Inference: Estimation and Hypothesis Testing	120
	5.1	Statistical Estimation (Confidence Intervals)	121
	5.2	Statistical Hypothesis Testing	131
	5.3	Comparison of Variances in Independent Samples	174
	5.4	Test of Equality of More than Two Variances	178
	5.5	Confidence Limits for a Variance	1/9
	5.0	I olerance Intervals	181
		Key Jellis	183
		References	185
6.	San	ple Size and Power	189
	6.1	Introduction	190

viii

Contents

	6.2	Determination of Sample Size for Simple Comparative	
		Experiments for Normally Distributed Variables	192
	6.3	Determination of Sample Size for Binomial Tests	199
	6.4	Determination of Sample Size to Obtain a Confidence	
		Interval of Specified Width	201
	6.5	Power	203
	6.6	Sample Size and Power for More than Two Treatments	207
	6.7	Sample Size for Bioequivalence Studies	210
		Key Terms	211
		Exercises	213
		References	214
7.	Line	ar Regression and Correlation	216
	7.1	Introduction	217
	7.2	Analysis of Standard Curves in Drug Analysis:	
		Application of Linear Regression	222
	7.3	Assumptions in Tests of Hypotheses in Linear	
•		Regression	224
	7.4	Estimate of the Variance: Variance of Sample	
		Estimates of the Parameters	225
	7.5	A Drug Stability Study: A Second Example of the	
		Application of Linear Regression	229
	7.6	Confidence Intervals in Regression Analysis	234
	7.7	Weighted Regression	239
	7.8	Analysis of Residuals	241
	7.9	Nonlinear Regression	243
	7.10	Correlation	248
	7.11	Comparison of Variances in Related Samples	257
		Key Terms	259
		Exercises	259
		References	263
8.	Ana	lysis of Variance	265
	8.1	One-Way Analysis of Variance	265
	8.2	Planned Versus a Posteriori (Unplanned) Comparisons	
		in ANOVA	274
	8.3	Another Example of One-Way Analysis of Variance:	
		Unequal Sample Sizes and the Fixed and Random	
		Models	286
	8.4	Two-Way Analysis of Variance (Randomized Blocks)	289

Contents

	8.5	Statistical Models**	306
	8.6	Analysis of Covariance**	308
	8.7	ANOVA for Pooling Regression Lines as Related to	
		Stability Data	315
		Key Terms	320
		Exercises	321
		References	325
9.	Fact	orial Designs**	326
	9.1	Definitions (Vocabulary)	326
	9.2	Two Simple Hypothetical Experiments to Illustrate the	
		Advantages of Factorial Designs	331
	9.3	Performing Factorial Experiments: Recommendations	
		and Notation	335
	9.4	A Worked Example of a Factorial Experiment	338
	9.5	Fractional Factorial Designs	345
	9.6	Some General Comments	351
		Key Terms	351
		Exercises	351
		References	354
10.	Trar	sformations and Outliers	355
	10.1	Transformations	356
	10.2	Outliers	369
		Key Terms	382
		Exercises	382
		References	383
11.	Exp	erimental Design in Clinical Trials	384
	11.1	Introduction	384
	11.2	Some Principles of Experimental Design and Analysis	385
	11.3	Parallel Design	391
	11.4	Crossover Designs and Bioavailability/Bioequivalence	
		Studies	397
	11.5	Repeated Measures (Split-Plot) Designs**	428
	11.6	Multiclinic Studies	435
	11.7	Interim Analyses	437

^{**}A more advanced topic.

Co	nte	nts
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	Key Terms	440
	Exercises	440
	References	442
12.	Quality Control	444
	12.1 Introduction	444
	12.2 Control Charts	445
	12.3 Acceptance Sampling and Operating Characteristic	
	Curves	463
	12.4 Statistical Procedures in Assay Development	467
	12.5 Establishing In-House Limits	478
	12.6 Some Statistical Aspects of Quality and the "Barr	
	Decision''	482
	Key Terms	487
	Exercises	487
	References	489
13.	Validation	490
	13.1 Process Validation	491
	13.2 Assay Validation	505
	13.3 Concluding Remarks	513
	Key Terms	513
	Exercises	. 513
	References	514
14.	Consumer Testing	515
	14.1 Introduction	515
	14.2 Product Comparisons	516
	14.3 Discrimination Tests: The Triangle Test	529
	Key Terms	535
	Exercises	535
	References	536
15.	Nonparametric Methods	537
	15.1 Data Characteristics and an Introduction to	
	Nonparametric Procedures	538
	15.2 Sign Test	541
	15.3 Wilcoxon Signed Rank Test	544
	15.4 Wilcoxon Rank Sum Test (Test for Differences	
	Between Two Independent Groups)	549

Co	nte	nts
----	-----	-----

	15.5	Kruskal–Wa	llis Test (One-Way ANOVA)	557
	15.6	Friedman Tes	st (Two-Way Analysis of Variance)	560
	15.7	Nonparametr	ic Analysis of Covariance	565
	15.8	Runs Test for	r Randomness	567
	15.9	Contingency	Tables	570
		Key Terms		584
		Exercises		584
		References		588
16.	Opti	mization Tec	hniques**	590
	16.1	Introduction		590
	16.2	Optimization	Using Factorial Designs	591
	16.3	Composite D	esigns to Estimate Curvature	604
	16.4	The Simplex	Lattice	610
	16.5	Sequential O	ptimization	619
		Key Terms	•	624
		Exercises		624
		References		625
Арр	endix	I: Some Pr	operties of the Variance	627
	I.1	Pooling Varia	ances	627
	I.2	Components	of Variance	628
	I.3	Variance of I	Linear Combinations of Independent	
		Variables	*	629
		Reference		630
Арр	endix	II: Compa	rison of Slopes and Testing of Linearity:	
		Determ	ination of Relative Potency	631
		Reference	:	637
Арр	endix	III: Multip	le Regression	638
		References		644
Арр	endix	IV: Tables		645
		Table IV.1 Table IV.2	Random Numbers Cumulative Normal Distribution:	645
			Cumulative Area Under the Normal	
			Distribution (Less Than or Equal to Z)	646

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