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## Non-linear Control Based on Physical Models

Electrical, Mechanical and Hydraulic Systems

With 47 Figures



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