

Design and Analysis of Experiments for Statistical Selection, Screening, and Multiple Comparisons

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