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## Observational Studies

With 14 Illustrations



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<sup>\*</sup> An asterisk indicates either an appendix of a section that has a footnote indicating that the section may be skipped without loss of continuity or deferred. The material in these sections is either a little more technical or a little more specialized or both. See the Preface, §2.

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