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Model Based Fuzzy Control

Fuzzy Gain Schedulers and
Sliding Mode Fuzzy Controllers

With 86 Figures



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