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Editor

On Einstein's Path

Essays in Honor of
Engelbert Schucking

With 11 Illustrations



Springer

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