

F.G. Major

The Quantum Beat

The Physical Principles of Atomic Clocks

With 230 Illustrations



Springer

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