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The Physics of Superconductors

Introduction to Fundamentals and Applications

with 114 Figures
and 51 Problems with Solutions

Springer

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