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# Self-Organization in Optical Systems and Applications in Information Technology

Second Edition  
With 105 Figures



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# Contents

## INTRODUCTION

<b>Self-Organization in Nonlinear Optics – Kaleidoscope of Patterns – M.A. Vorontsov and W.B. Miller . . . . .</b>	<b>1</b>
1 What Is This Book About? . . . . .	1
2 Nonlinear Optics: The Good Old Times . . . . .	3
3 The First Model – Kerr-Slice/Feedback Mirror System . . . . .	3
4 Diffusion, Diffraction, and Spatial Scales . . . . .	5
5 One More Scheme: The First Step Toward Optical Synergetics . . . . .	6
6 Nonlocal Interactions; Optical Kaleidoscope of Patterns . . . . .	7
7 OK-Equation and “Dry Hydrodynamics” . . . . .	9
8 One More Nonlinear Element: Two-Component Optical Reaction-Diffusion Systems . . . . .	10
9 Diffraction at Last; Rolls and Hexagons . . . . .	12
10 <i>d</i> iffraction and <i>D</i> iffraction . . . . .	13
11 Far Away from Hexagons: Delay in Time and Space . . . . .	16
12 Diffusion + Diffraction + (Interference) + Nonlocal Interactions = Akhseals . . . . .	18
References . . . . .	22

## CHAPTER 1

<b>Information Processing and Nonlinear Physics: From Video Pulses to Waves and Structures – S.A. Akhmanov . . . . .</b>	<b>27</b>
1 Information Encoding by Carrier Modulation and the Physics of Nonlinear Oscillations and Waves . . . . .	27
2 Modulation of Light Waves and Information Encoding in Digital Optical Computers. Optical Triggers . . . . .	29
3 Strong Optical Nonlinearities. Nonlinear Materials . . . . .	35
4 Generation and Transformation of Femtosecond Light Pulses . . . . .	36
5 Control of Transverse Interactions in Nonlinear Optical Resonators: Generation, Hysteresis, and Interaction of Nonlinear Structures . . . . .	38
6 Conclusion. Nonlinear Optics and Molecular Electronics . . . . .	40
References . . . . .	43

## CHAPTER 2

**Optical Design Kit of Nonlinear Spatial Dynamics –**

<b>E.V. Degtiarev and M.A. Vorontsov . . . . .</b>	<b>45</b>
1 Elementary Optical Synergetic Blocks . . . . .	46
1.1 Characteristics of a Synergetic Block . . . . .	46
1.2 Optical Synergetic Block Based on LCLV . . . . .	47
1.3 Main Mathematical Models . . . . .	50
1.4 Optical Multistability and Switching Waves . . . . .	52
2 Integral Transverse Interactions . . . . .	54
2.1 The Synergetic Optical Block with an Electronic Feedback Circuit . . . . .	54
3 Optical Counterparts of Two-Component Reaction-Diffusion Systems . . . . .	56
3.1 Linear Stability Analysis and Bifurcation of Uniform States . .	60
4 Conclusion . . . . .	64
References . . . . .	66

## CHAPTER 3

**Pattern Formation in Passive Nonlinear Optical Systems –**

<b>W.J. Firth . . . . .</b>	<b>69</b>
1 Induced and Spontaneous Patterns . . . . .	71
1.1 Materials and Geometries . . . . .	72
2 Mirror Feedback Systems . . . . .	73
2.1 Kerr Slice with Feedback Mirror . . . . .	74
2.2 Basic Model and Stability Analysis . . . . .	75
2.3 Liquid Crystal Light Valve Systems . . . . .	81
3 Pattern Formation in Optical Cavities . . . . .	82
3.1 Vector Kerr Model and Equations . . . . .	83
3.2 Spatial Stability of Symmetric Solutions . . . . .	84
3.3 Pattern Formation in a Two-Level Optical Cavity . . . . .	89
4 Conclusion . . . . .	93
References . . . . .	94

## CHAPTER 4

**Spatio-Temporal Instability Threshold Characteristics in Two-Level Atom Devices – M. Le Berre, E. Ressayre, and**

<b>A. Tallet . . . . .</b>	<b>97</b>
1 Linear Stability Analysis of Stationary Solutions . . . . .	100
2 Feedback Mirror Experiment . . . . .	104
2.1 Experimental Results . . . . .	104
2.2 Linear Analysis . . . . .	105
2.3 Static and Dynamical Thresholds . . . . .	107
2.4 Role of the Longitudinal Grating . . . . .	109

2.5 Discussion of the Phase Conjugation Effects . . . . . 109

2.6 Role of the Homogeneous Dephasing Time . . . . . 112

2.7 Role of the Time Delay . . . . . 114

3 The Ségard and Macke Experiment . . . . . 114

3.1 Experiment . . . . . 114

3.2 Linear Analysis . . . . . 115

3.3 Physics of the Coupling . . . . . 116

3.4 No Rabi Gain at Threshold . . . . . 117

4 Rayleigh Self-Oscillation in an Intrinsic System . . . . . 118

4.1 Characteristics of the Self-Oscillation in the No-Pump  
Depletion Model . . . . . 119

4.2 Threshold Characteristics for Depleted Pump Fields . . . . . 123

4.3 Doppler Effect . . . . . 125

5 Conclusion . . . . . 126

References . . . . . 128

CHAPTER 5

**Transverse Traveling-Wave Patterns and Instabilities in Lasers**

– Q. Feng, R. Indik, J. Lega, J.V. Moloney, A.C. Newell,  
and M. Staley . . . . . 133

1 Basic Equations and Transverse Traveling-Wave Solution . . . . 134

2 Instabilities: Direct Stability Analysis and Phase Equations . . . 137

3 Pattern Transition and Selection . . . . . 143

4 Conclusion . . . . . 144

References . . . . . 145

CHAPTER 6

**Laser-Based Optical Associative Memories – M. Brambilla,  
L.A. Lugiato, M.V. Pinna, F. Pratti, P. Pagani, and  
P. Vanotti . . . . . 147**

1 Nonlinear Dynamic Equations and Steady-State Equations . . . 149

2 Single- and Multimode Stationary Solutions.  
Spatial Multistability . . . . . 152

3 Operation with Injected Signal . . . . . 154

4 General Description of the System . . . . . 155

References . . . . . 158

CHAPTER 7

**Pattern and Vortex Dynamics in Photorefractive Oscillators**  
– F.T. Arecchi, S. Boccaletti, G. Giacomelli, P.L. Ramazza,  
and S. Residori . . . . . 161

1 Pattern Formation and Complexity . . . . . 163

1.1 The Multimode Optical Oscillator: 1-, 2-, 3-Dimensional  
Optics . . . . . 163

1.2	The Photorefractive Ring Oscillator. How to Control the Fresnel Number . . . . .	167
1.3	Periodic (PA) and Chaotic (CA) Alternation and Space-Time Chaos . . . . .	170
2	Phase Singularities, Topological Defects, and Turbulence . . . . .	174
2.1	Phase Singularities in Linear Waves. Speckle Experiments . . . . .	174
2.2	Phase Singularities in Nonlinear Optics: Scaling Laws . . . . .	178
2.3	Comparison of Vortex Statistics in Speckle and Photorefractive Patterns . . . . .	185
2.4	Transition from Boundary- to Bulk-Controlled Regimes . . . . .	190
3	Theory of Pattern Formation and Pattern Competition . . . . .	197
3.1	Equations of Photorefractive Oscillator . . . . .	197
3.2	Truncation to a Small Number of Modes: Numerical Evidence of PA, CA, and STC . . . . .	203
3.3	Symmetry Breaking at the Onset of Pattern Competition . . . . .	208
	References . . . . .	212

## CHAPTER 8

**From the Hamiltonian Mechanics to a Continuous Media. Dissipative Structures. Criteria of Self-Organization –**

<b>Yu. L. Klimontovich</b> . . . . .	217	
1	The Transition from Reversible Equations of Mechanics to Irreversible Equations of the Statistical Theory . . . . .	218
1.1	Physical Definition of Continuous Medium . . . . .	218
1.2	The Gibbs Ensemble for Nonequilibrium Processes . . . . .	220
1.3	The Unified Definition of “Continuous Medium” Averaging over Physically Infinitesimal Volume . . . . .	220
1.4	The Constructive Role of the Dynamic Instability of the Motion of Atoms . . . . .	221
2	The Unified Description of Kinetic and Hydrodynamic Motion . . . . .	222
2.1	The Generalized Kinetic Equation . . . . .	222
3	The Equation of Entropy Balance. The Heat Flow . . . . .	224
4	Equations of Hydrodynamics with Self-Diffusion . . . . .	225
5	Effect of Self-Diffusion on the Spectra of Hydrodynamic Fluctuations . . . . .	227
6	The Kinetic Approach in the Theory of Self-Organization – Synergetics. Basic Mathematical Models . . . . .	228
7	Kinetic and Hydrodynamic Description of the Heat Transfer in Active Medium . . . . .	230
8	Kinetic Equation for Active Medium of Bistable Elements . . . . .	231
9	Kinetic Fluctuations in Active Media . . . . .	233
9.1	The Langevin Source in the Kinetic Equation . . . . .	233
9.2	Spatial Diffusion. “Tails” in the Time Correlations . . . . .	233

9.3	The Langevin Source in the Reaction Diffusion (FKPP) Equation . . . . .	234
10	Natural Flicker Noise (“1/f Noise”) . . . . .	235
10.1	Natural Flicker Noise for Diffusion Processes . . . . .	235
10.2	Natural Flicker Noise for Reaction-Diffusion Processes . . . . .	237
11	Criteria of Self-Organization . . . . .	238
11.1	Evolution in the Space of Controlling Parameters. S-Theorem . . . . .	238
11.2	The Comparison of the Relative Degree of Order of States on the Basis of the S-Theorem Using Experimental Data . . . . .	240
12	Conclusion. Associative Memory and Pattern Recognition . . . . .	241
	References . . . . .	242
<b>Index</b>	. . . . .	<b>245</b>