

**State-Space Models with Regime Switching**  
Classical and Gibbs-Sampling Approaches with Applications

Chang-Jin Kim and Charles R. Nelson

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# Contents

	Preface and Acknowledgments	xi
<b>1</b>	<b>Introduction</b>	<b>1</b>
	1.1 State-Space Models and Markov Switching in Econometrics: A Brief History	2
	1.2 Computer Programs and Data References	4
<b>I</b>	<b>THE CLASSICAL APPROACH</b>	<b>7</b>
<b>2</b>	<b>The Maximum Likelihood Estimation Method: Practical Issues</b>	<b>9</b>
	2.1 Maximum Likelihood Estimation and the Covariance Matrix of $\hat{\theta}_{ML}$	9
	2.2 The Prediction Error Decomposition and the Likelihood Function	11
	2.3 Parameter Constraints and the Covariance Matrix of $\hat{\theta}_{ML}$ References	13 17
<b>3</b>	<b>State-Space Models and the Kalman Filter</b>	<b>19</b>
	3.1 Time-Varying-Parameter Models and the Kalman Filter	19
	3.2 State-Space Models and the Kalman Filter	29
	3.3 Application 1: A Decomposition of Real GDP and the Unemployment Rate into Stochastic Trend and Transitory Components	37
	3.4 Application 2: An Application of the Time- Varying-Parameter Model to Modeling Changing Conditional Variance	44
	3.5 Application 3: Stock and Watson's Dynamic Factor Model of the Coincident Economic Indicators Appendix: GAUSS Programs to Accompany Chapter 3 References	48 55 56
<b>4</b>	<b>Markov-Switching Models</b>	<b>59</b>
	4.1 Introduction: Serially Uncorrelated Data and Switching	59
	4.2 Serially Correlated Data and Markov Switching	64
	4.3 Issues Related to Markov-Switching Models	68
	4.4 Application 1: Hamilton's Markov-Switching Model of Business Fluctuations	78

4.5	Application 2: A Unit Root in a Three-State Markov-Switching Model of the Real Interest Rate	82
4.6	Application 3: A Three-State Markov-Switching Variance Model of Stock Returns	86
	Appendix: GAUSS Programs to Accompany Chapter 4	93
	References	93
<b>5</b>	<b>State-Space Models with Markov Switching</b>	97
5.1	Specification of the Model	98
5.2	The Basic Filter and Estimation of the Model	99
5.3	Smoothing	106
5.4	An Evaluation of the Kim Filter and Approximate MLE	109
5.5	Application 1: Sources of Monetary Growth Uncertainty and Economic Activity	115
5.6	Application 2: Friedman's Plucking Model of Business Fluctuations and Implied Business Cycle Asymmetry	124
5.7	Application 3: A Dynamic Factor Model with Markov Switching: Business Cycle Turning Points and a New Coincident Index	126
	Appendix: GAUSS Programs to Accompany Chapter 5	133
	References	135
<b>6</b>	<b>State-Space Models with Heteroskedastic Disturbances</b>	139
6.1	State-Space Models with ARCH Disturbances	140
6.2	State-Space Models with Markov-Switching Heteroskedasticity	146
6.3	Application 1: The Link between the Inflation Rate and Inflation Uncertainty	151
6.4	Application 2: Transient Fads and the Crash of '87 in the U.S. Stock Market	157
	Appendix: GAUSS Programs to Accompany Chapter 6	166
	References	167
<b>II</b>	<b>THE GIBBS-SAMPLING APPROACH</b>	169
<b>7</b>	<b>An Introduction to Bayesian Inference and Gibbs-Sampling</b>	171
7.1	Classical versus Bayesian Analysis: Fundamental Differences	171

7.2	Bayesian Analysis: An Introduction	173
7.3	Gibbs-Sampling: Motivation and Basic Idea	178
7.4	Examples of Gibbs-Sampling in Econometrics	180
	Appendix: GAUSS Programs to Accompany Chapter 7	188
	References	188
<b>8</b>	<b>State-Space Models and Gibbs-Sampling</b>	189
8.1	Generating the State Vector When $Q$ Is Positive-Definite	190
8.2	Generating the State Vector When $Q$ Is Singular: A Generalization	194
8.3	Application 1: A Gibbs-Sampling Approach to a Linear Dynamic Factor Model and a New Coincident Index	196
	Appendix: GAUSS Program to Accompany Chapter 8	205
	References	208
<b>9</b>	<b>Markov-Switching Models and Gibbs-Sampling</b>	209
9.1	A Basic Model and the Bayesian Gibbs-Sampling Approach	209
9.2	Application 1: A Three-State Markov-Switching Variance Model of Stock Returns	219
9.3	Application 2: A Three-State Markov Switching Mean-Variance Model of the Real Interest Rate	229
	Appendix: GAUSS Programs to Accompany Chapter 9	236
	References	236
<b>10</b>	<b>State-Space Models with Markov Switching and Gibbs-Sampling</b>	237
10.1	General Framework	237
10.2	Application 1: Business Cycle Turning Points and a New Coincident Index	241
10.3	Application 2: Business Cycle Duration Dependence within a Dynamic Factor Model: An Advantage of the Gibbs-Sampling Approach over the Classical Approach	257
10.4	Application 3: An Unobserved Components Model of the Long-Run U.S./U.K. Real Exchange Rate with Heteroskedasticity	266
	Appendix: GAUSS Program to Accompany Chapter 10	271
	References	272

<b>11</b>	<b>Gibbs-Sampling and Parameter Uncertainty:</b>	
	<b>Testing for Mean Reversion in Heteroskedastic Data</b>	<b>275</b>
11.1	Alternative Ways of Incorporating Parameter Uncertainty	275
11.2	Variance Ratio Tests of Mean Reversion: A Review	278
11.3	Historical Pattern of Heteroskedasticity and the Sampling Distribution of the Variance Ratio Statistic	279
11.4	New Tests of Mean Reversion in the Presence of Heteroskedasticity	284
	Appendix: GAUSS Programs to Accompany Chapter 11	292
	References	293
	Index	295