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The Crystal Lattice

Phonons, Solitons, Dislocations



Berlin \cdot Weinheim \cdot New York \cdot Chichester \cdot Brisbane \cdot Singapore \cdot Toronto

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