
Principles of Physical Chemistry

Understanding Molecules, Molecular Assemblies, Supramolecular Machines

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