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# INTRODUCTION TO OPTICAL WAVEGUIDE ANALYSIS

Solving Maxwell's Equations and  
the Schrödinger Equation

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