

# Optical Propagation in Linear Media

*Atmospheric Gases and Particles,  
Solid-State Components, and Water*

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