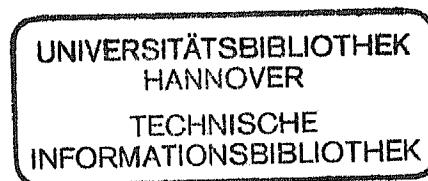


# Nuclear Magnetic Resonance of Liquid Crystals

edited by

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D. Reidel Publishing Company

Dordrecht / Boston / Lancaster

Published in cooperation with NATO Scientific Affairs Division

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