

Mathematical Aspects of Superspace

edited by

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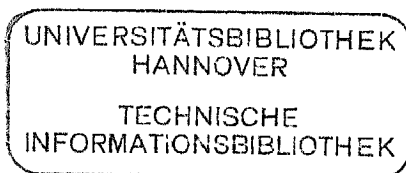
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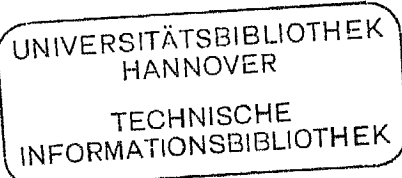
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TABLE OF CONTENTS

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Preface	ix
J. WESS	
Non-linear Realization of Supersymmetry	1
1. Introduction	1
2. The Akulov-Volkov field	1
3. Superfields	5
4. Standard fields	7
5. $N > 1/N = 1$	9
6. $N = 1$ supergravity	11
References	12
C.J.S. CLARKE	
Fields, Fibre Bundles and Gauge Groups	15
1. Manifolds	15
2. Fibre bundles	17
2.1 Fields	17
2.2 Coordinate bundles	18
2.3 Fibre bundles	19
2.4 Examples	19
2.5 Fields and geometry	21
2.6 Principal bundles	22
2.7 Cross-sections	23
2.8 Bundles with structure: sheaves	24
2.9 Associated bundles	25
2.10 Connections	27
2.11 Examples	30
3. Gauge Groups	31
3.1 Proposition: Gauge transformations	31
3.2 Gauge action on associate bundles	32
3.3 Quasi-gauge groups	33
3.4 Gauge algebras	34
3.5 Gauge-invariance	35
3.6 Gauge theory	38



4. Space-Time	38
4.1 Spinors	38
4.2 Soldering forms	40
4.3 Achtbeine	41
4.4 Example: Lie derivatives	42
4.5 Supersymmetries	43
K.D. ELWORTHY	
Path Integration on Manifolds	47
1. Introduction	48
2. Gaussian measures, cylinder set measures, and the Feynman-Kac formula	50
2.1 Basic difficulties; terminology	50
2.2 Gaussian measures	53
2.3 Cylinder set measures	57
2.4 Radonification	60
2.5 Feynman-Kac formula	62
2.6 Time slicing	65
3. Feynman path integrals	66
3.1 Oscillatory integrals and Fresnel integrals	66
3.2 Feynman maps	67
3.3 Feynman path integrals and the Schrödinger equation	69
4. Path integration on Riemannian manifolds	70
4.1 Wiener measure and rolling without slipping	70
4.2 The Pauli-Van-Vleck-De Witt propagator	78
5. Gauge invariant equations; diffusion and differential forms	80
5.1 Quantum particle in a classical magnetic field	80
5.2 Heat equation for differential forms	83
Acknowledgements, References	85
M. BATCHELOR	
Graded Manifolds and Supermanifolds	91
Preface and cautionary note	91
0. Standard notation	91
1. The category GM	94
1.1 Definitions and examples of graded manifolds	94

1.2 Bundles in GM	98
2. The geometric approach	105
2.1 The general idea	105
2.2 The graded commutative algebra B and supereuclidan space	106
2.3 Smooth maps on $E^{r,s}$	108
2.4 Examples of supermanifolds	113
2.5 Bundles over supermanifolds	116
3. Comparisons	120
3.1 Comparing GM and SSM	120
3.2 Comparison of geometric manifolds	123
3.3 A direct method of comparing GM and G^∞	124
4. Lie supergroups	127
4.1 Lie supergroups in the geometric categories	127
4.2 Graded Lie groups	129
Table: "All I know about supermanifolds"	130
References	133
A. ROGERS	
Aspects of the Geometrical Approach to Supermanifolds	135
1. Abstract	135
2. Building superspace over an arbitrary spacetime	137
3. Super Lie groups	140
4. Compact supermanifolds with non-Abelian fundamental group	43
5. Developments and applications	143
References	146
A. ROGERS	
Integration on Supermanifolds	149
1. Introduction	149
2. Standard integration theory	149
3. Integration over odd variables	151
4. Superforms	154
5. Integration on $E^{r,s}$	156
6. Integration on supermanifolds	158
References	159

R.J. BLATTNER, J.H. RAWNSLEY	
Remarks on Batchelor's Theorem	161
J. ISENBERG, D. BAO, P.B. YASSKIN	
Classical Supergravity	173
Introduction	174
1. Definition of classical supergravity	176
2. Dynamical analysis of classical field theories	182
3. Formal dynamical analysis of classical supergravity	186
4. The exterior algebra formulation of classical supergravity	195
5. Does classical supergravity make sense?	200
Appendix: Notations and conventions	200
References	203
List of participants	207
Index	209