



Structural Concrete

**Textbook on Behaviour, Design and
Performance**

Updated knowledge of the CEB/FIP Model Code 1990

**Volume 2
Basis of design**

July 1999

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