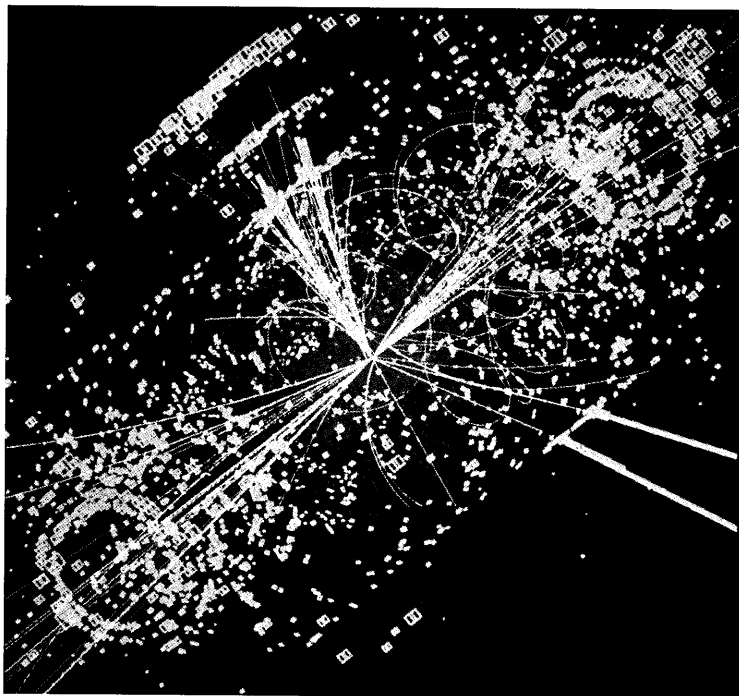


EFFECTIVE FIELD THEORIES



Alexey A. Petrov • Andrew E. Blechman

Wayne State University, USA

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