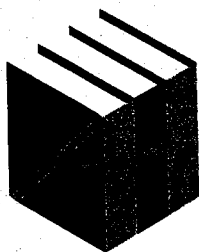


Principles of GNSS, Inertial, and Multisensor Integrated Navigation Systems

Second Edition

Paul D. Groves



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