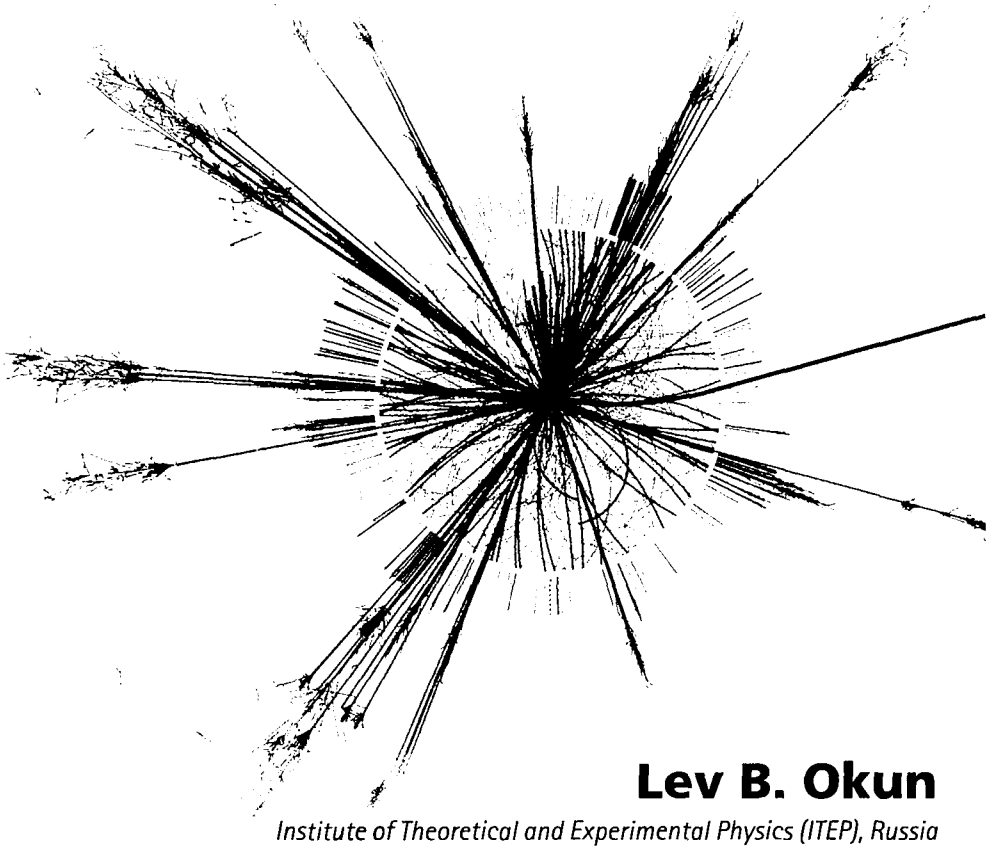
LEPTONS AND QUARKS

Special Edition Commemorating the Discovery of the Higgs Boson



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World Scientific

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About the Author