

Roger Penrose

**THE EMPEROR'S  
NEW MIND**

Concerning Computers, Minds  
and The Laws of Physics

FOREWORD BY  
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