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# Granular-Relational Data Mining

How to Mine Relational Data in the Paradigm of Granular Computing?

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