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Optimal Sampled-Data Control Systems

With 222 Figures



London Berlin Heidelberg New York Paris Tokyo Hong Kong Barcelona Budapest

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