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# **Neural Networks for Modelling and Control of Dynamic Systems**

## **A Practitioner's Handbook**

With 84 Figures

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