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Additional resources supporting the Catalyzing Change Series are available at [www.nctm.org/change](http://www.nctm.org/change).