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Nonlinear Filters

Estimation and Applications

Second Revised and Enlarged Edition

With 18 Figures
and 45 Tables



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