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Testing for Random Walk Coefficients in Regression and State Space Models

With 38 Figures
and 72 Tables

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