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Coherent Atomic Manipulation and Cooling

Interferometric Laser Cooling and Composite
Pulses for Atom Interferometry

Doctoral Thesis accepted by
the University of Southampton, UK

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